



INTERNATIONAL PRESTRESSED
HOLLOWCORE ASSOCIATION



Hegger + Partner
Ingenieurbüro für Tragwerksplanung
und Bauberatung

Shear resistance of hollow core slabs Testing and Design

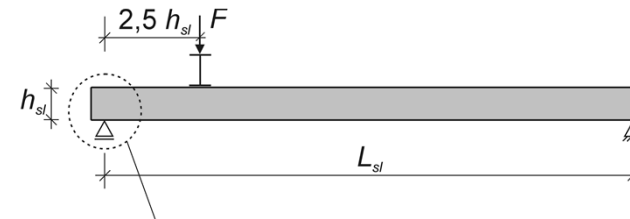
Technical Seminar in Aachen 26./27.10.2011



Dipl.-Ing. Hans-Peter Doser

- testing arrangement

- execution
- material properties

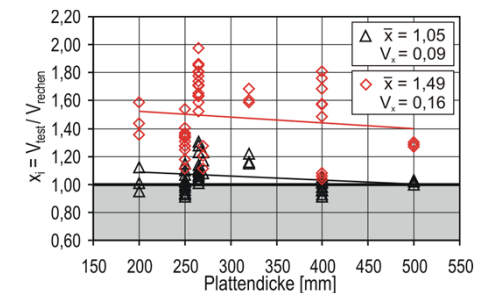


- testing evaluation

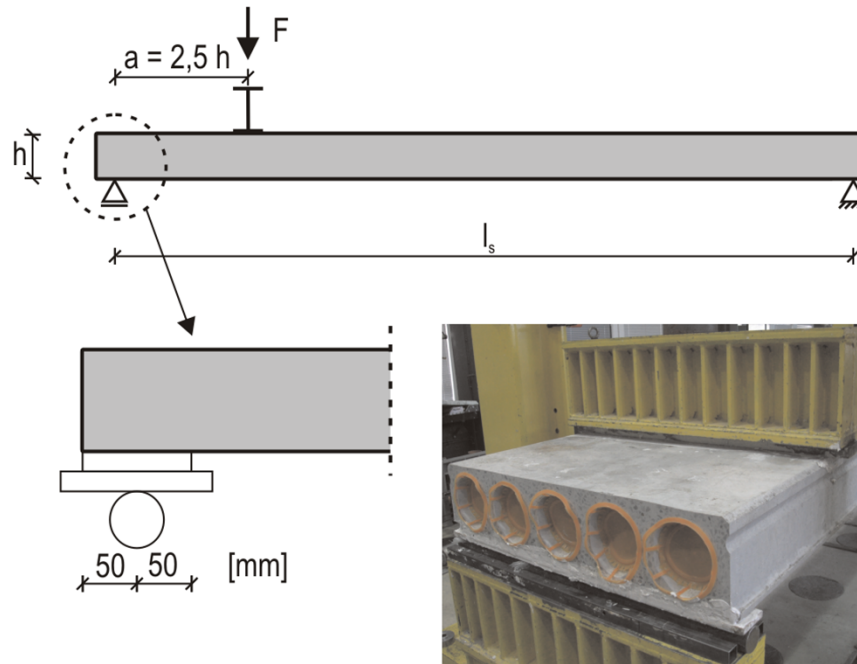
- German approvals
- EN 1168:2009

$$V_{Rd,ct} = f \cdot \frac{I_y \cdot b_w}{S_y} \left(\sqrt{\left(\frac{f_{ctk;0,05}}{\gamma_c} \right)^2 - \alpha_1 \cdot \sigma_{cd} \cdot \frac{f_{ctk;0,05}}{\gamma_c}} - \alpha_p \cdot \tau_{cpd} \right)$$

- data base and statistical evaluation



Testing arrangement



- According to EN 1168 (one line loading)
- Length of specimen: $l = 15 \times h$; min = 4,0 m
- Distance of load: $a = 2,5 \times h$
- Load application via stiff girder on gypsum

Pictures of test



Testing execution

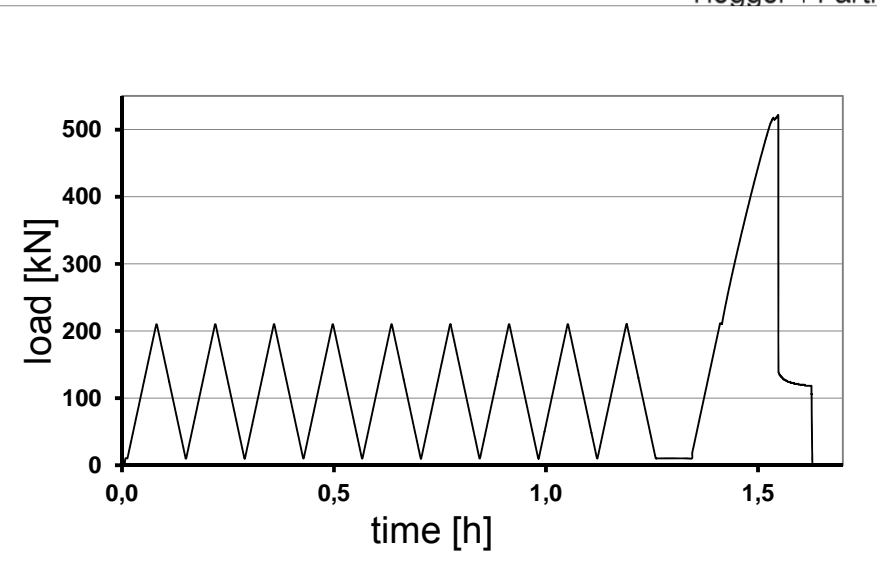
German approval

9 load cycles up to $0,91 \times V_{Rd,ctm}$

$$V_{Rd,ctm}(f_{ctm}, \gamma=1,8)$$

Increasing load to failure

$$V_{Rk,ctm}(f_{ctm}, \gamma=1,0)$$



EN 1168

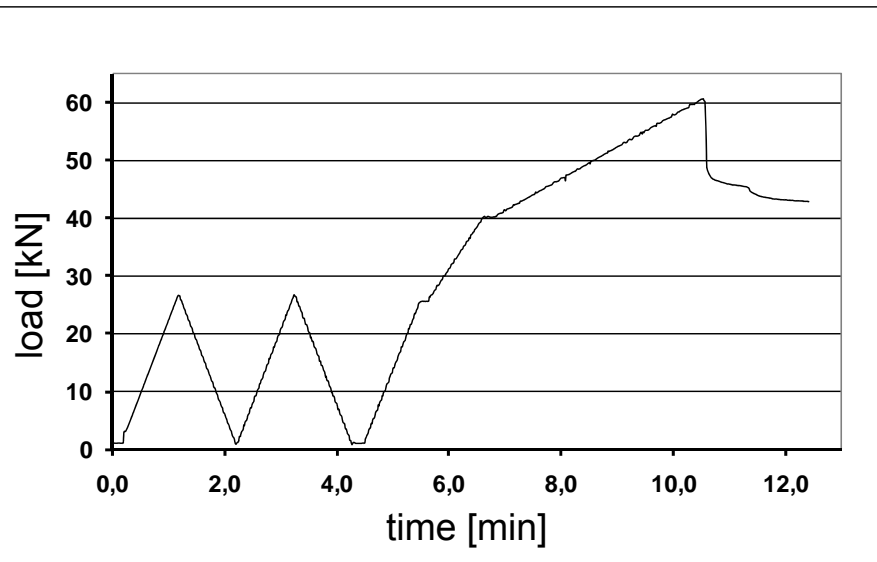
2 load cycles up to $0,70 \times V_{Rd,ct}$

$$V_{Rd,ct}(f_{ctk;0,05}, \gamma=1,8)$$

Stepwise increasing load

50% $V_{Rk,ctm}$ – 75% $V_{Rk,ctm}$ – failure

$$V_{Rk,ctm}(f_{ctm}, \gamma=1,0)$$



Material samples

- Concrete cubes 150x150x150mm
- Drill cores taken vertically out of the webs



Material properties

Determination of tensile strength



drilled cores



i-section
(„dog bones“)

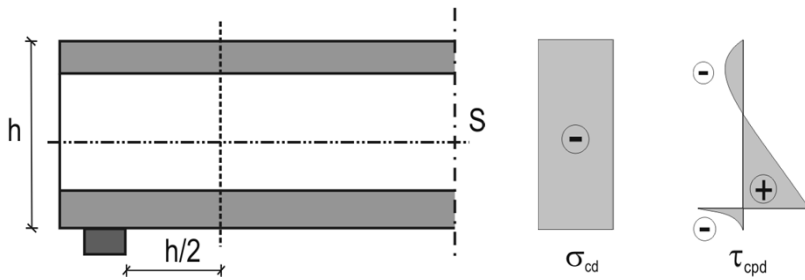


Adhesive tensile
strength

design equations

German approvals (DIBt)

$$V_{Rd,ct} = f \cdot \frac{I_y \cdot b_w}{S_y} \left(\sqrt{\left(\frac{f_{ctk;0,05}}{\gamma_c} \right)^2 - \alpha_1 \cdot \sigma_{cd} \cdot \frac{f_{ctk;0,05}}{\gamma_c}} - \alpha_p \cdot \tau_{cpd} \right)$$



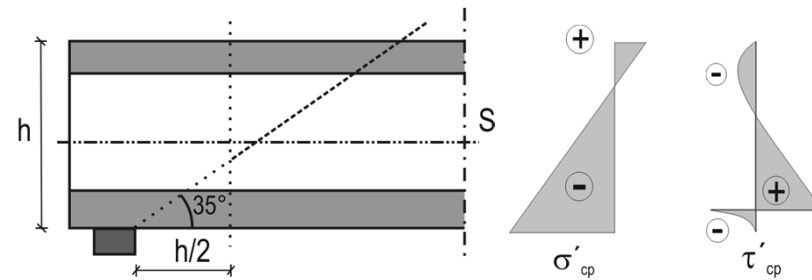
calculation of stress components

$$\sigma_{cd} = \frac{N_{Ed}}{A}$$

$$\tau_{cpd} = \frac{T_{M-M}}{I_{bpd} \cdot b_{M-M}} \quad T_{M-M} = \sum \sigma_{x,p} \cdot h_m \cdot b_i$$

DIN EN 1168

$$V_{Rd,c} = \frac{I_y \cdot b_w}{S_y} \left(\sqrt{f_{ctd}^2 + \sigma'_{cp} \cdot f_{ctd}} - \tau'_{cp} \right)$$



calculation of stress components

$$\sigma'_{cp} = \sum_{i=1}^n \left[\alpha_i \cdot \left(\frac{P_{xi}}{A} + \frac{P_{xi} \cdot e_i}{I_y} \cdot z \right) \right] + \frac{M_{Ed}}{I_y} \cdot z$$

$$\tau'_{cp} = \frac{1}{b_w} \sum_{i=1}^n \left[\frac{dP_{xi}}{dx} \cdot \left(\frac{A_0}{A} - \frac{S_y \cdot e_i}{I_y} - C_{pt} \right) \right]$$

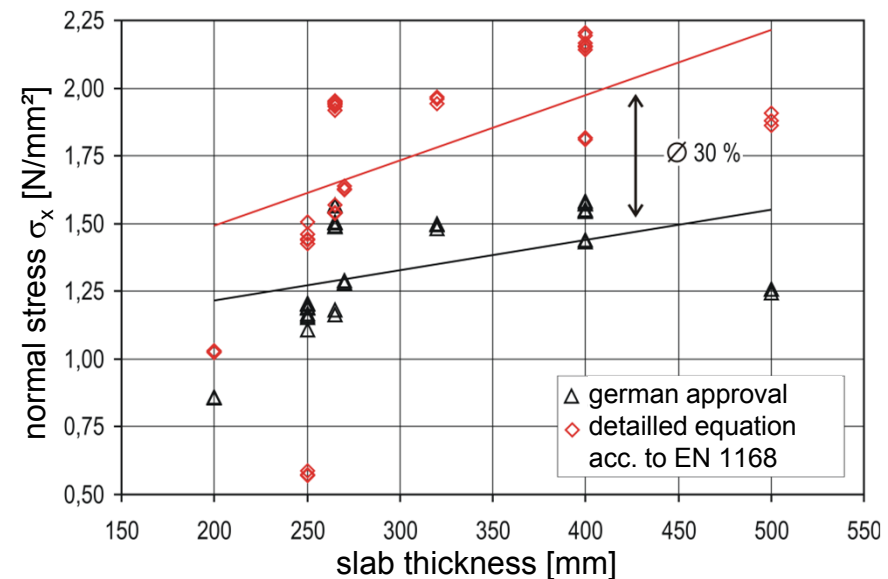
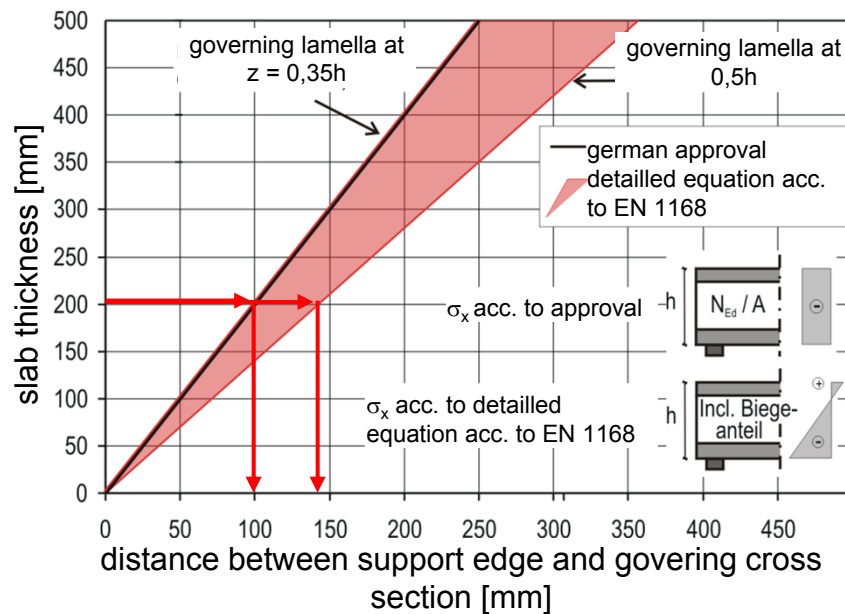
simplified equation:

$$V_{Rd,c} = \varphi \cdot \frac{I_y \cdot b_w}{S_y} \sqrt{f_{ctd}^2 + \beta \cdot \alpha_l \cdot \sigma_{cp} \cdot f_{ctd}}$$

Normal stress σ_{cd}

Differences in calculating σ_{cd}

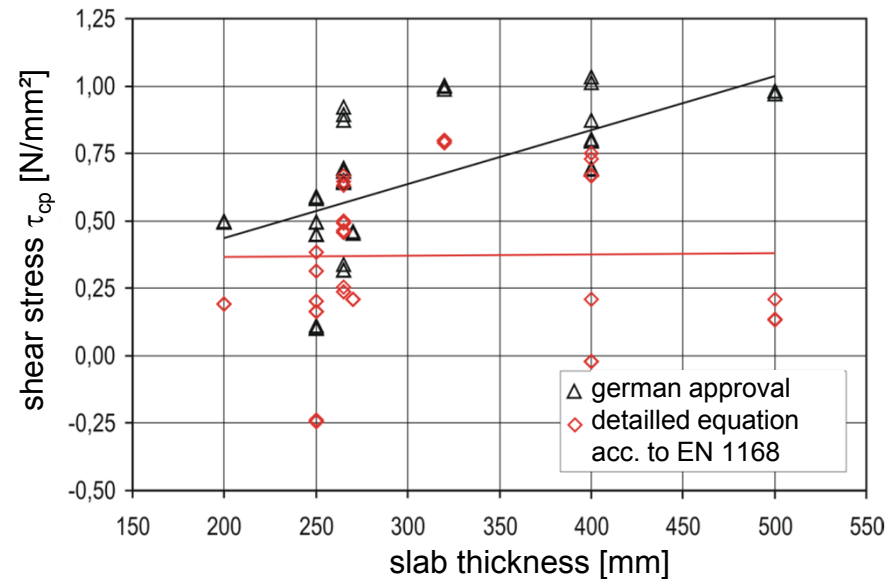
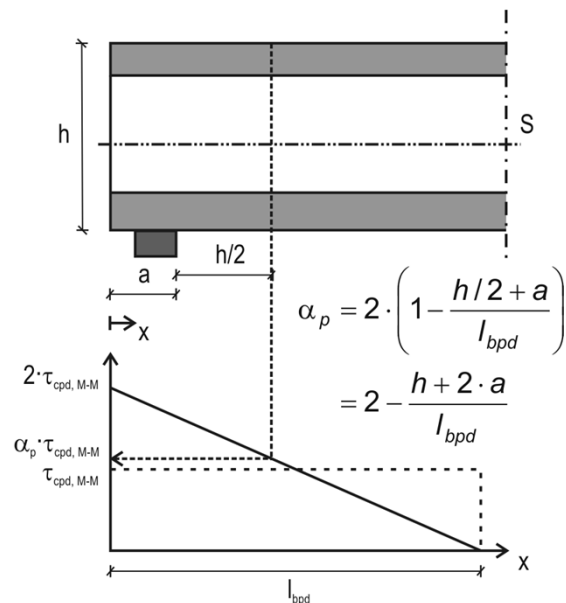
- Constant normal stress in gov. cross section (approval)
- Linearly distr. normal stress (consideration of bending moments due to prestress) (DIN EN 1168)
- Consideration of increasing prestressing force



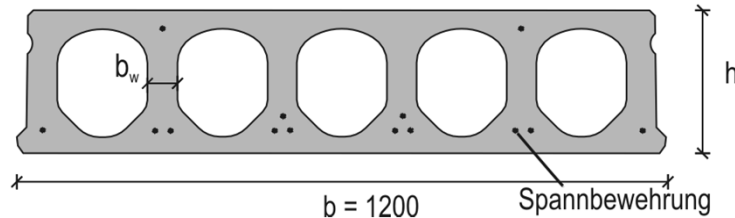
shear stress τ_{cp}

Differences in consideration of τ_{cpd}

- modification factor α_p increases τ_{cpd} in most cases (for $(a + h/2) < 0,5 l_{bpd}$)
- EN 1168 considers τ_{cpd} independent of the distance to bearing
- Vertical distance to critical point determines value of τ_{cpd}



cross section



$h \sim 200 - 500 \text{ mm}$

$\Sigma b_w/b \sim 0,2 - 0,4$

prestress steel

number of strands

loss of prestress

material properties

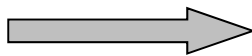
concrete class C45/55

test results tension ($n \approx 250$)

test parameters

slab length

ultimate loads

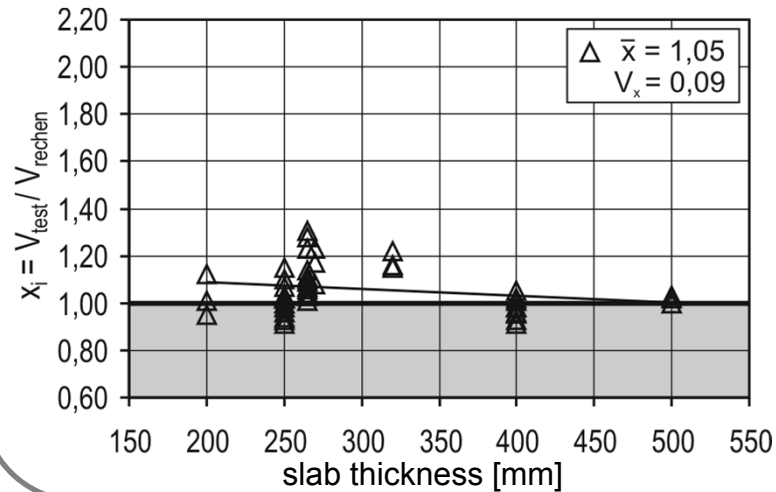


~70 tests carried through by H+P at imb

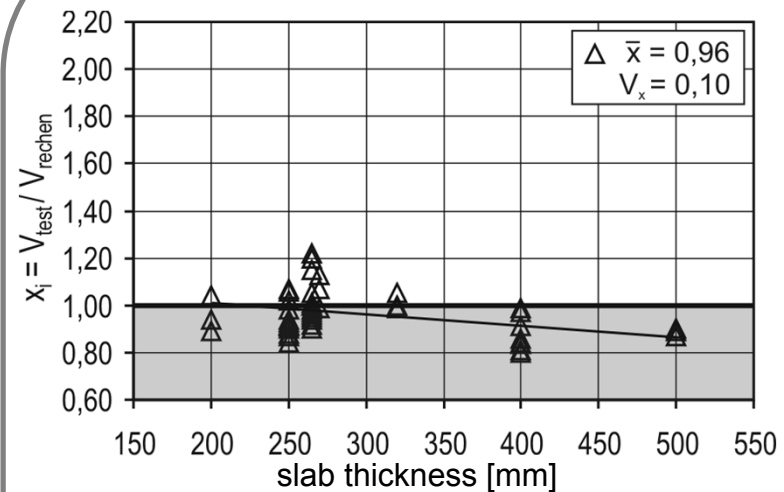
48 test with shear tension failure

Safety factor

German approval (DIBt)



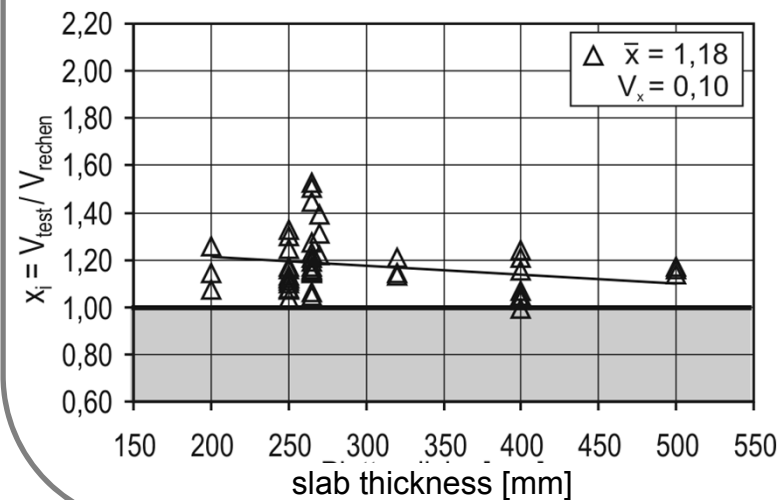
DIN EN 1168



detailed

$$x_i = V_{\text{test}} / V_{\text{calc}}, i = 1, \dots, 48$$

Δ V_{calc} with $f_{\text{ctm, test}}$



simplified