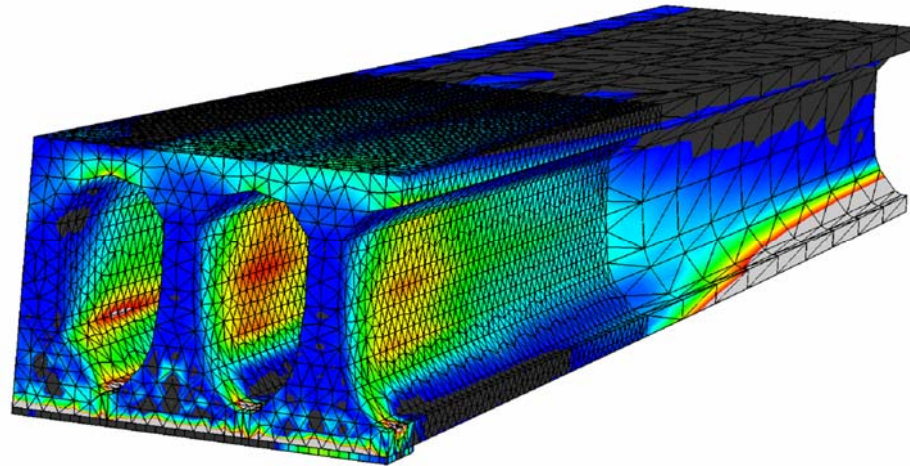


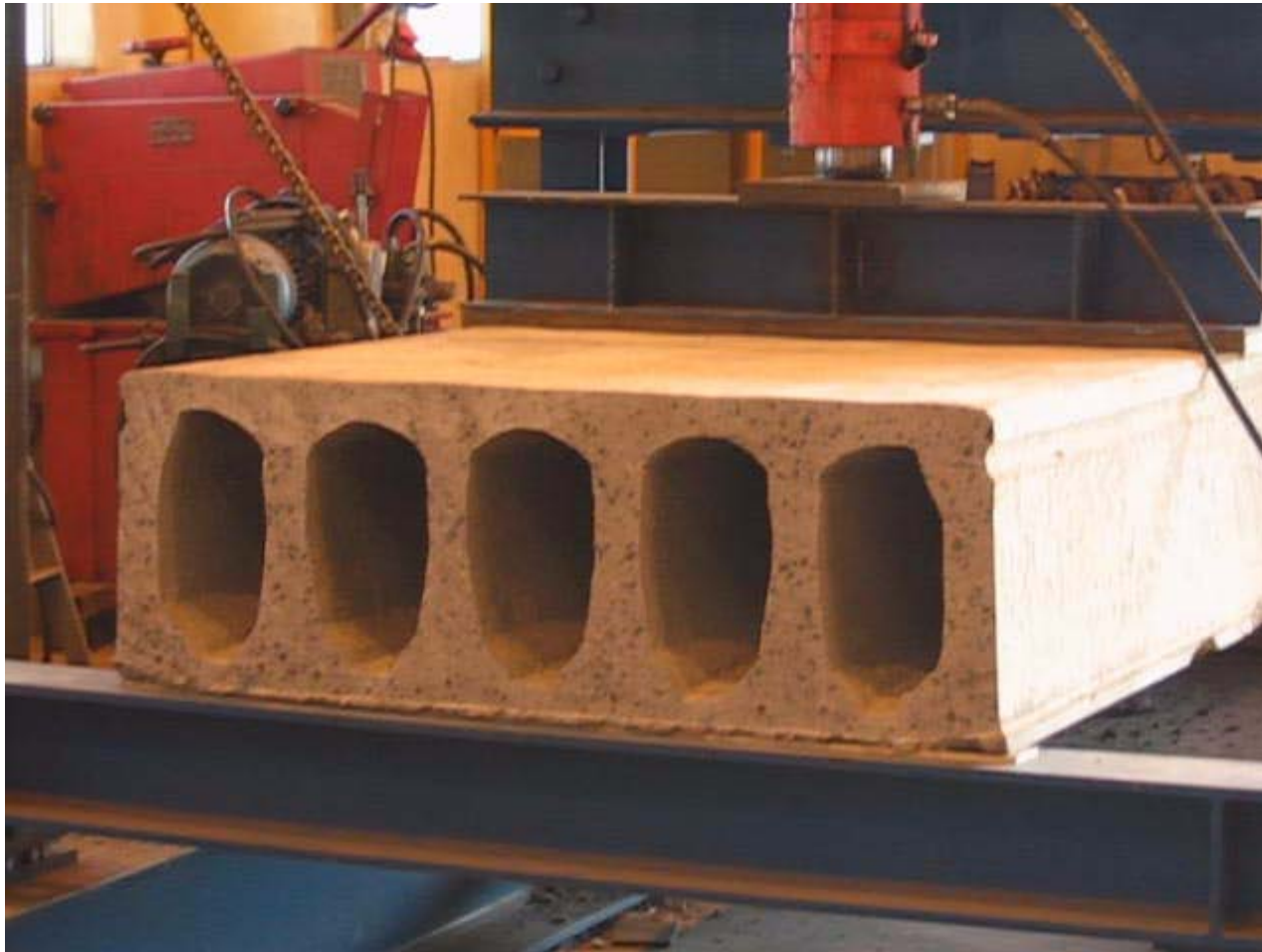
# Parametric Study of Web Shear Cracking

Based on the Master's Project "*Improved Design Method for Web Shear Tension Failure in Hollow Core Units*" in the International Master's Programme Structural Engineering



**Lars Rettne**

# Web Shear Tension Failure in Hollow Core Units



# Problem Description

”In the present standard the guidance on how to calculate shear tension capacity is not detailed enough and a more precise method is needed”

# Aim of the Project

- Create finite element (FE) models of single hollow core units
- Perform calculations using Yang's method of single hollow core units
- Compare the shear capacity and location of the critical point between the two methods

# Critical Point

= The point where web shear cracking starts

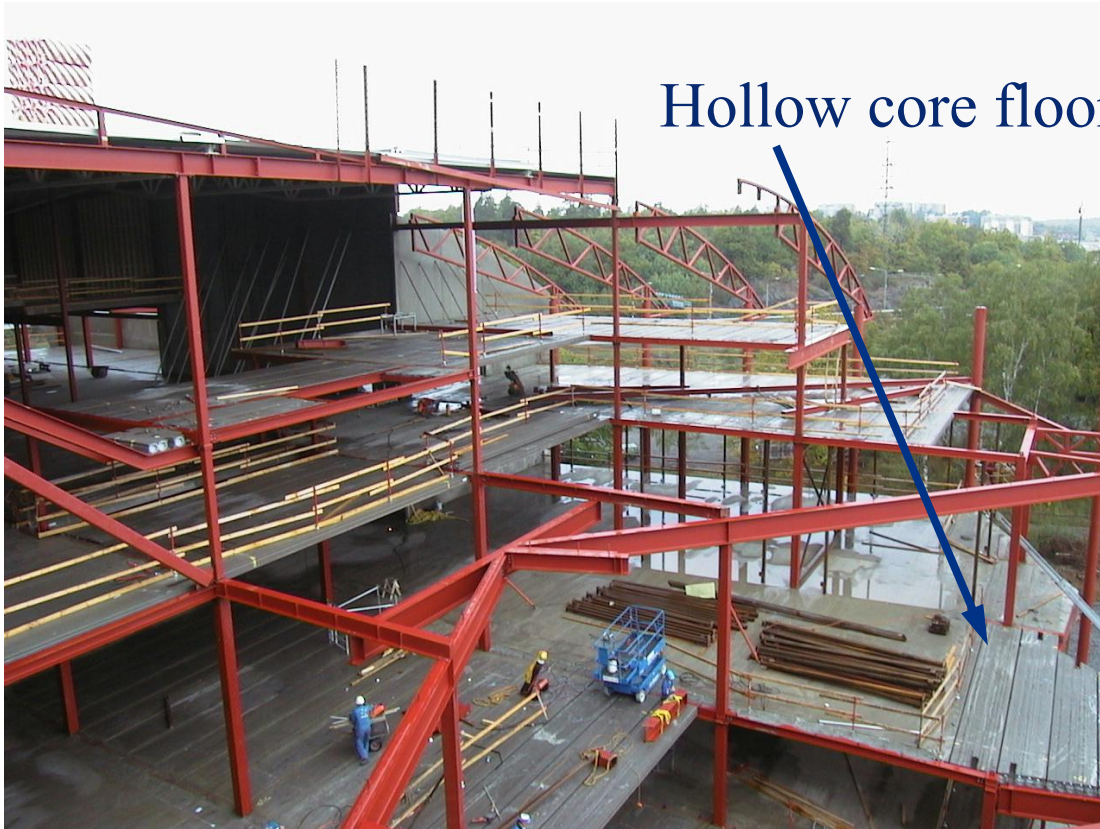


# Collaboration

- This project was initiated by Strängbetong, which is the largest hollow core unit producer in Sweden

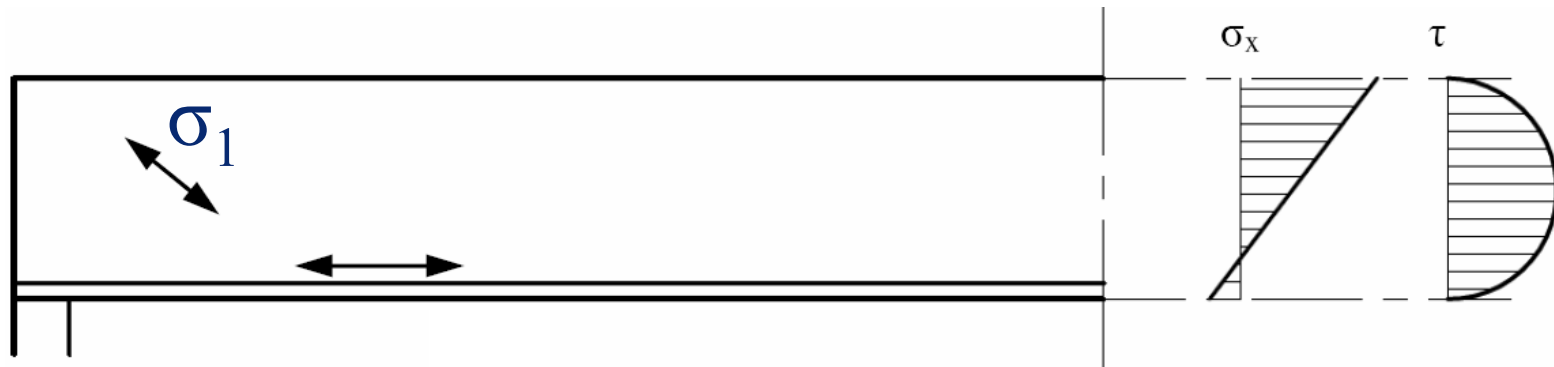
# Hollow Core Floors

Hollow core floors consist of hollow core units



# Web Shear Tension Failure in Hollow Core Units

Uncracked cross-section



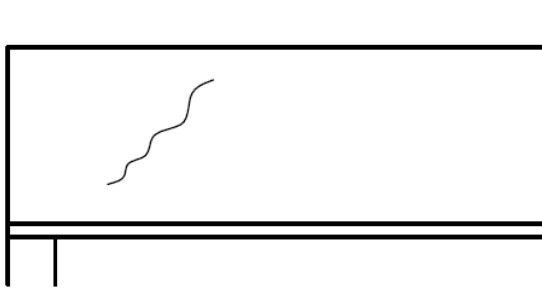
$\sigma_1$  = Principal stress

$f_{ctm}$  = Mean tensile strength of concrete

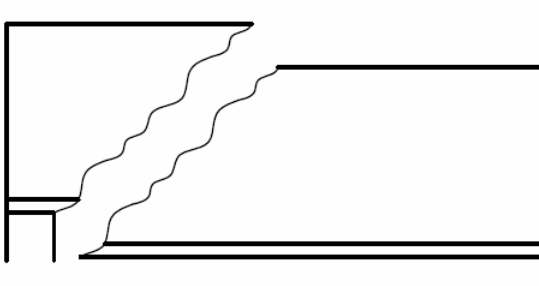


# Web Shear Tension Failure in Hollow Core Units

Web shear cracking



Immediately failure (brittle)



$$\sigma_1 = f_{ctm}$$

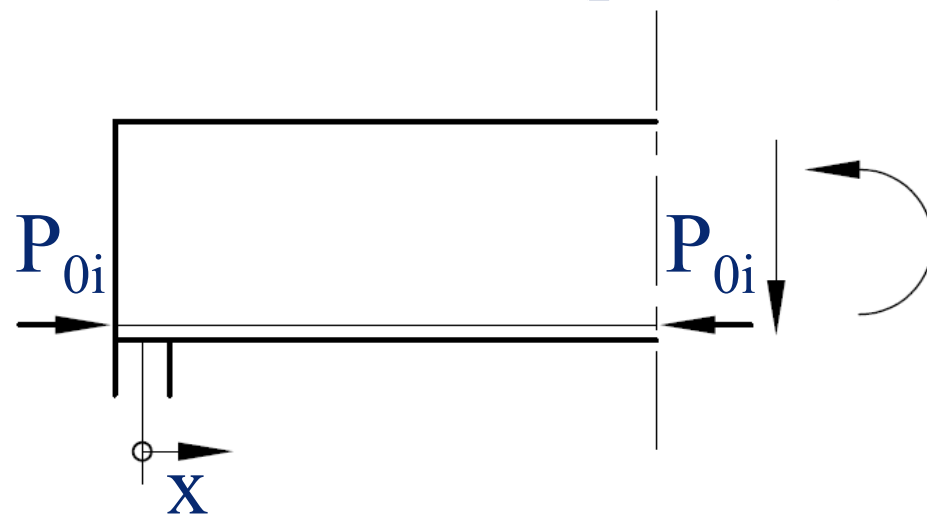


# Shear Capacity with Respect to Web Shear Tension Failure

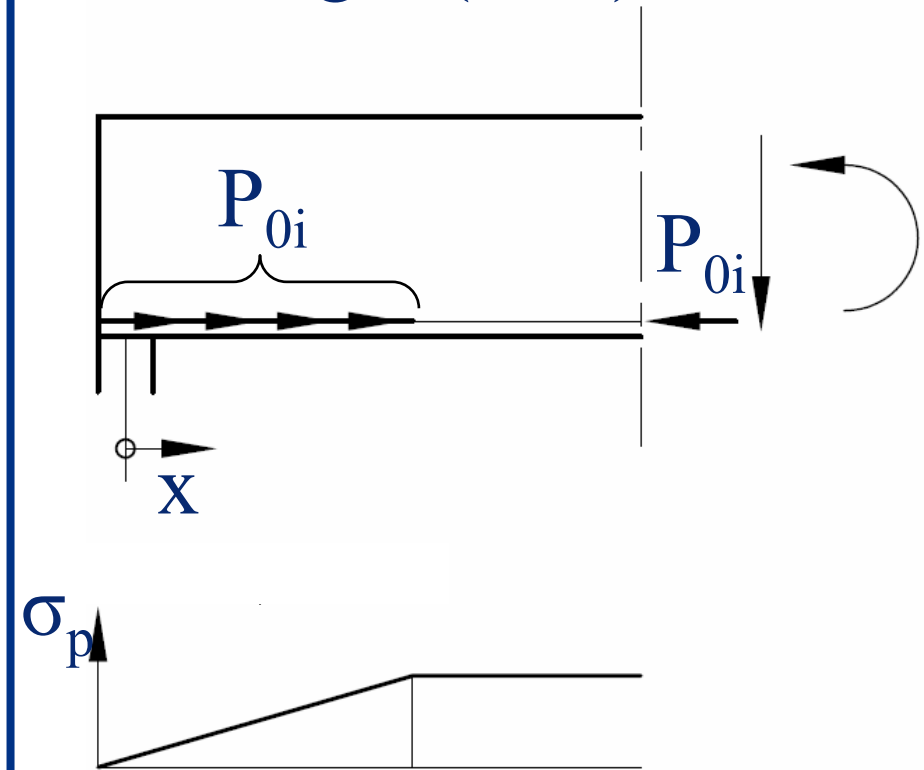
- Failure when the concrete tensile strength is reached,  $\sigma_1 = f_{ctm}$
- The principal stresses are dependent of the shear and normal stresses,  $\sigma_1 = \sigma_1(\sigma_x, \tau)$

# Shear Stress Calculations in Prestressed Members

## Traditional (present)



## Yang's (new)



# Shear Stress Calculations in Prestressed Members

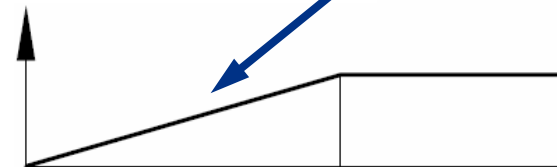
Traditional (present)

$$\tau(x_{cp}, z_{cp}) = \frac{S(z_{cp})V(x_{cp})}{I_I b_w(z_{cp})}$$

Yang's (new)

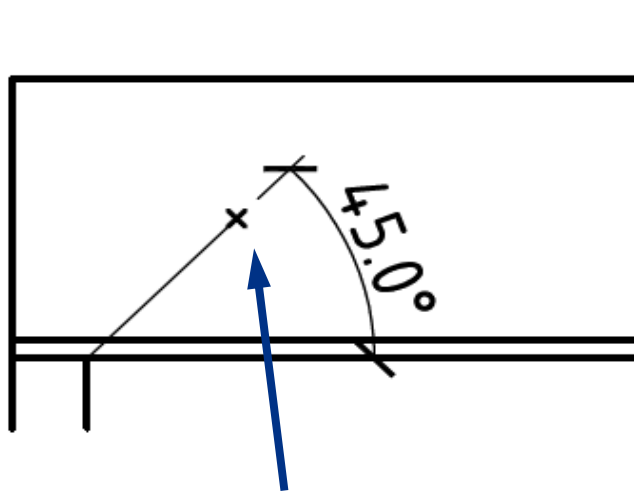
$$\tau(x_{cp}, z_{cp}) = \frac{S(z_{cp})V(x_{cp})}{I_I b_w(z_{cp})} + f\left(\frac{dP_{0i}}{dx}\right)$$

The shape is taken  
into account



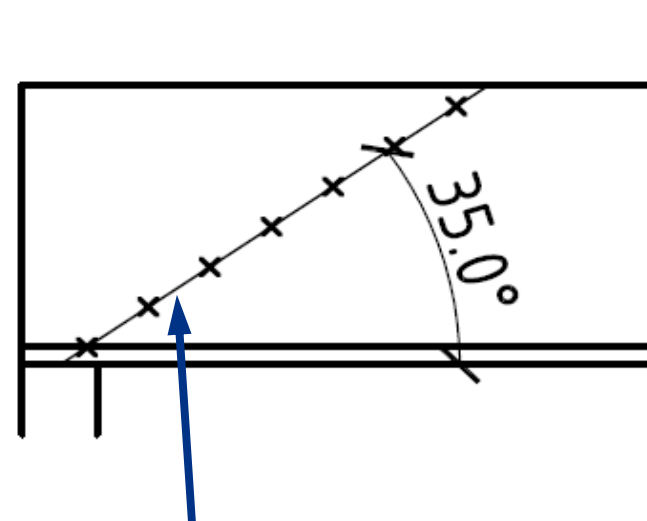
# Shear Capacity Calculations in Prestressed Members

Traditional (present)



Assumed location of critical point

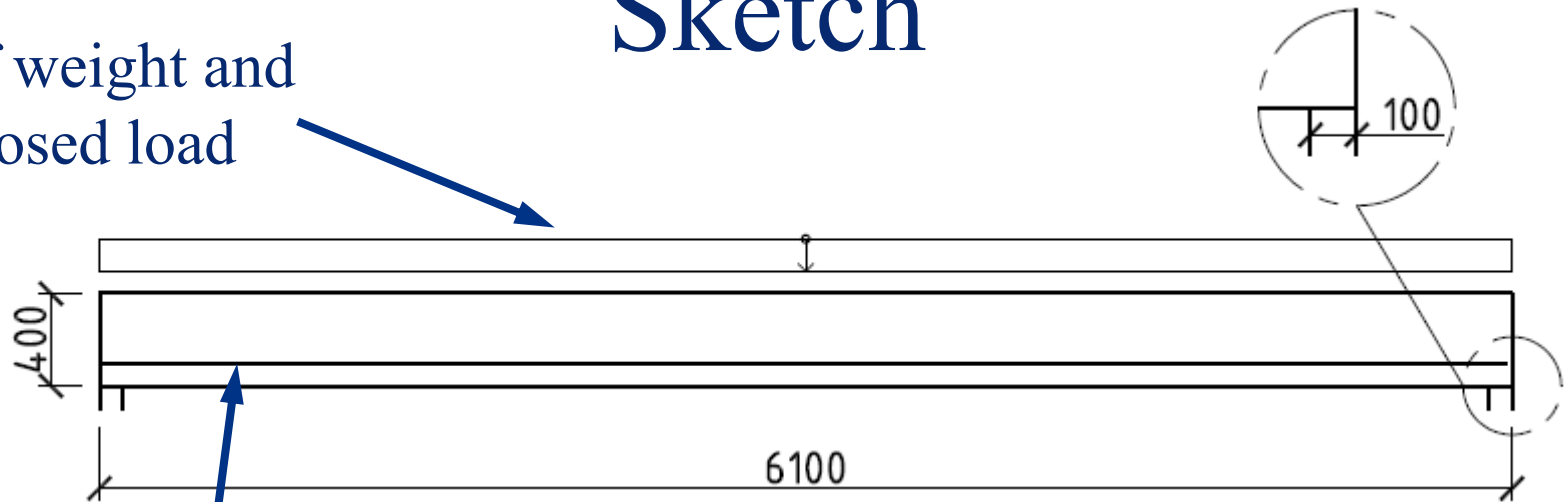
Yang's (new)



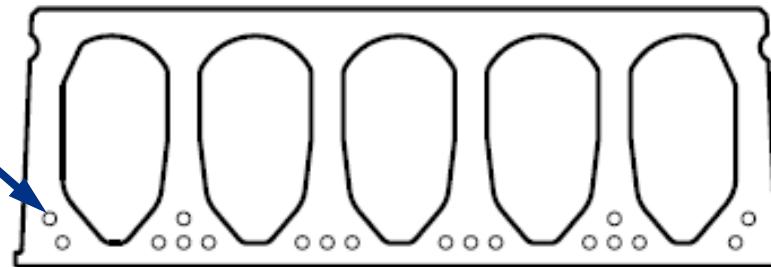
Assumed location of critical point somewhere along line

# Reference Case – Principal Sketch

Self weight and imposed load



Prestressing strand



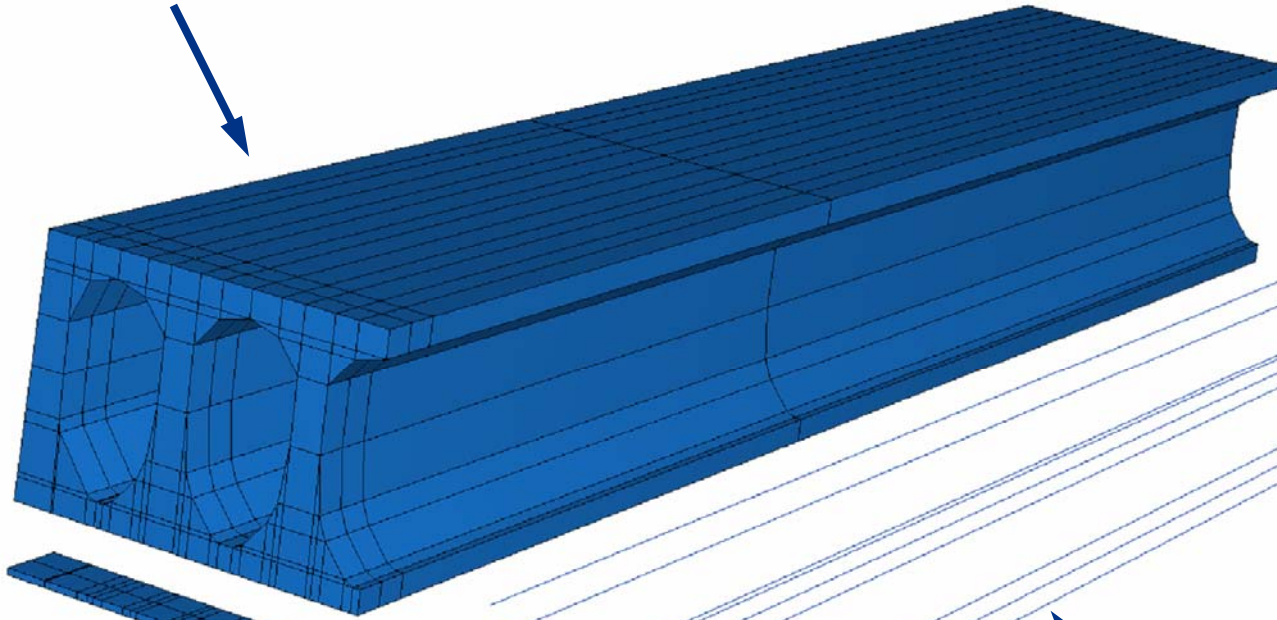
Cross-section

# Parametric Study

- Prestressing strand arrangement
- Prestressing strand amount
- Prestress
- Concrete strength class
- Concrete strength at strand release
- Prestress transfer function
- Type of cross-section

# FE Model

Concrete part: Solid finite elements

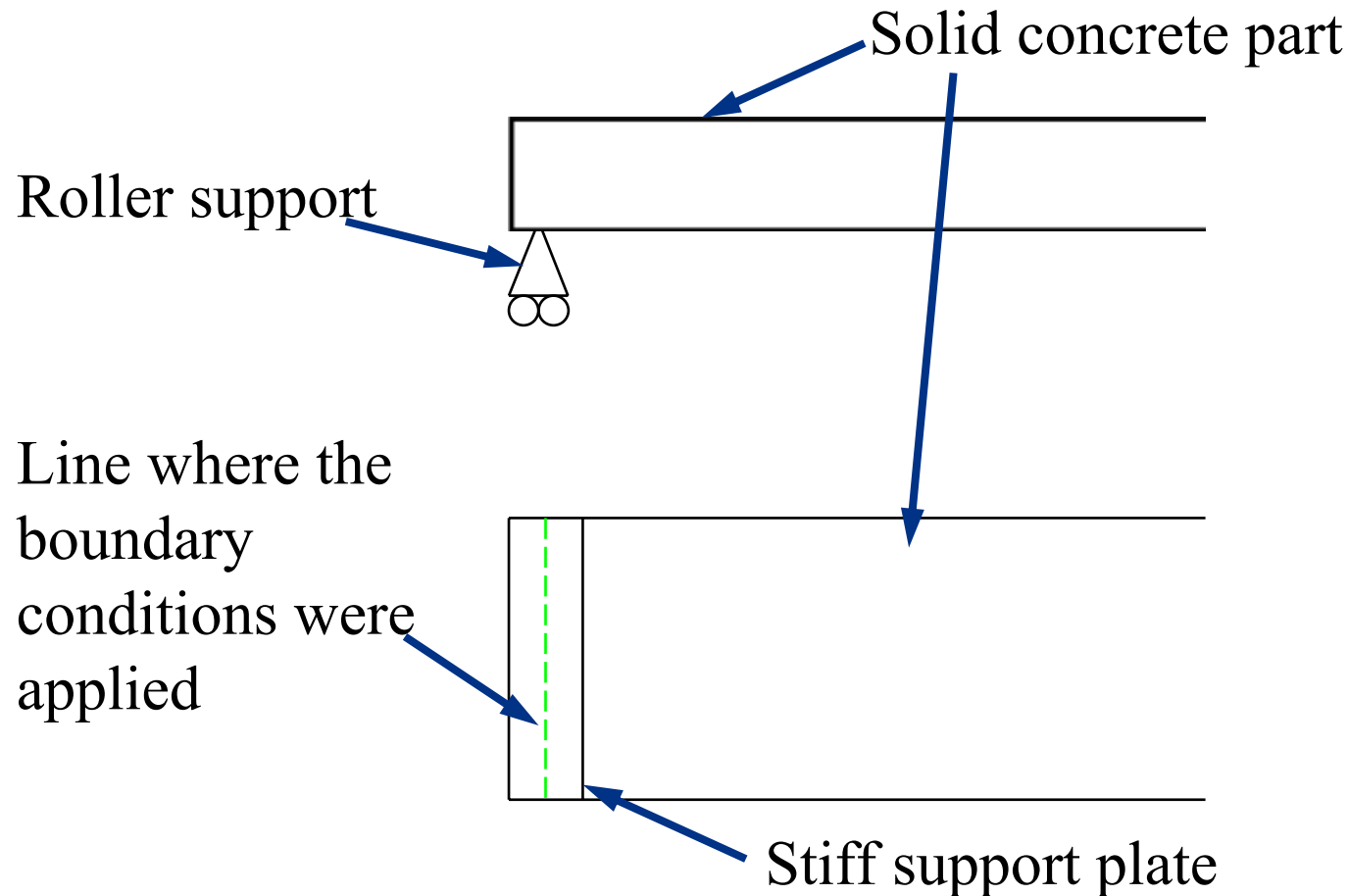


Steel strands: Truss finite elements

Stiff steel support plate: Solid finite elements

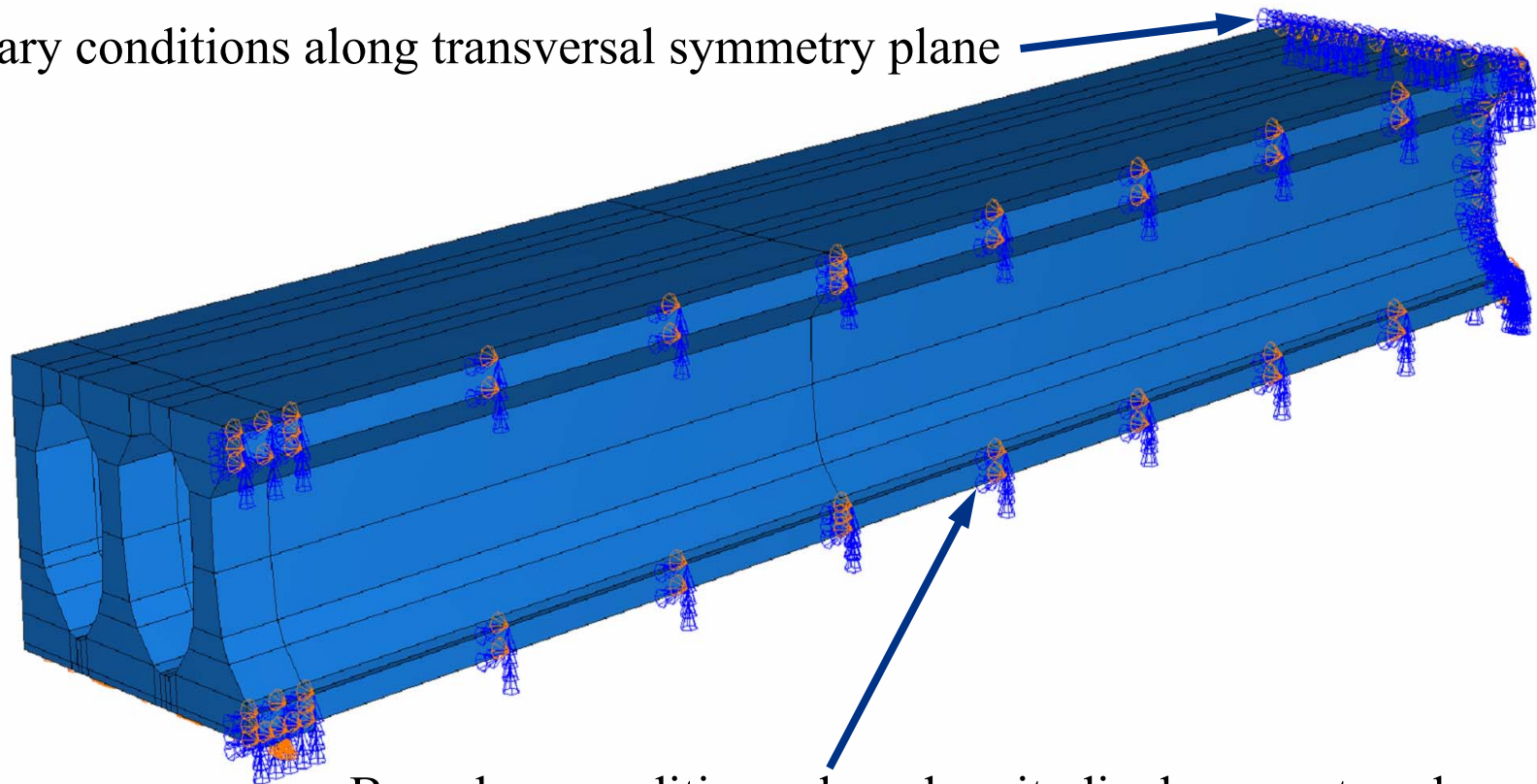


# FE Model - Boundary Conditions



# FE Model - Boundary Conditions: Symmetry Planes

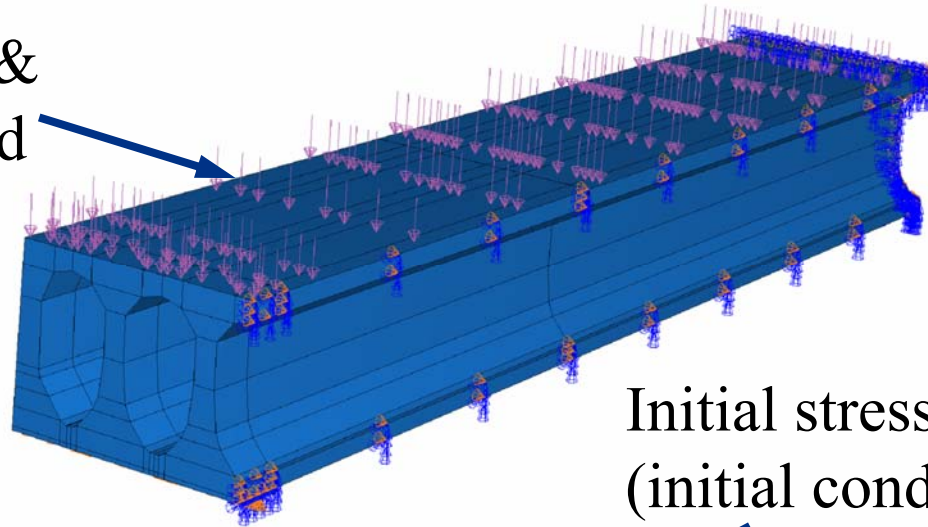
Boundary conditions along transversal symmetry plane



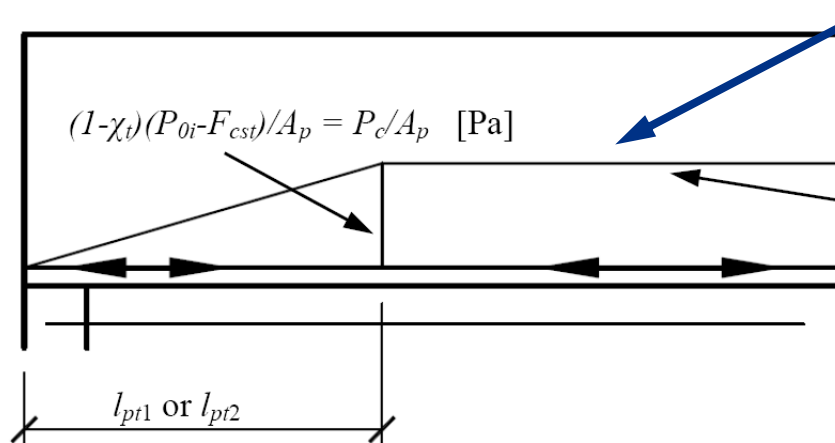
Boundary conditions along longitudinal symmetry plane

# FE Model - Loads

Self weight &  
Imposed load  
(pressure)



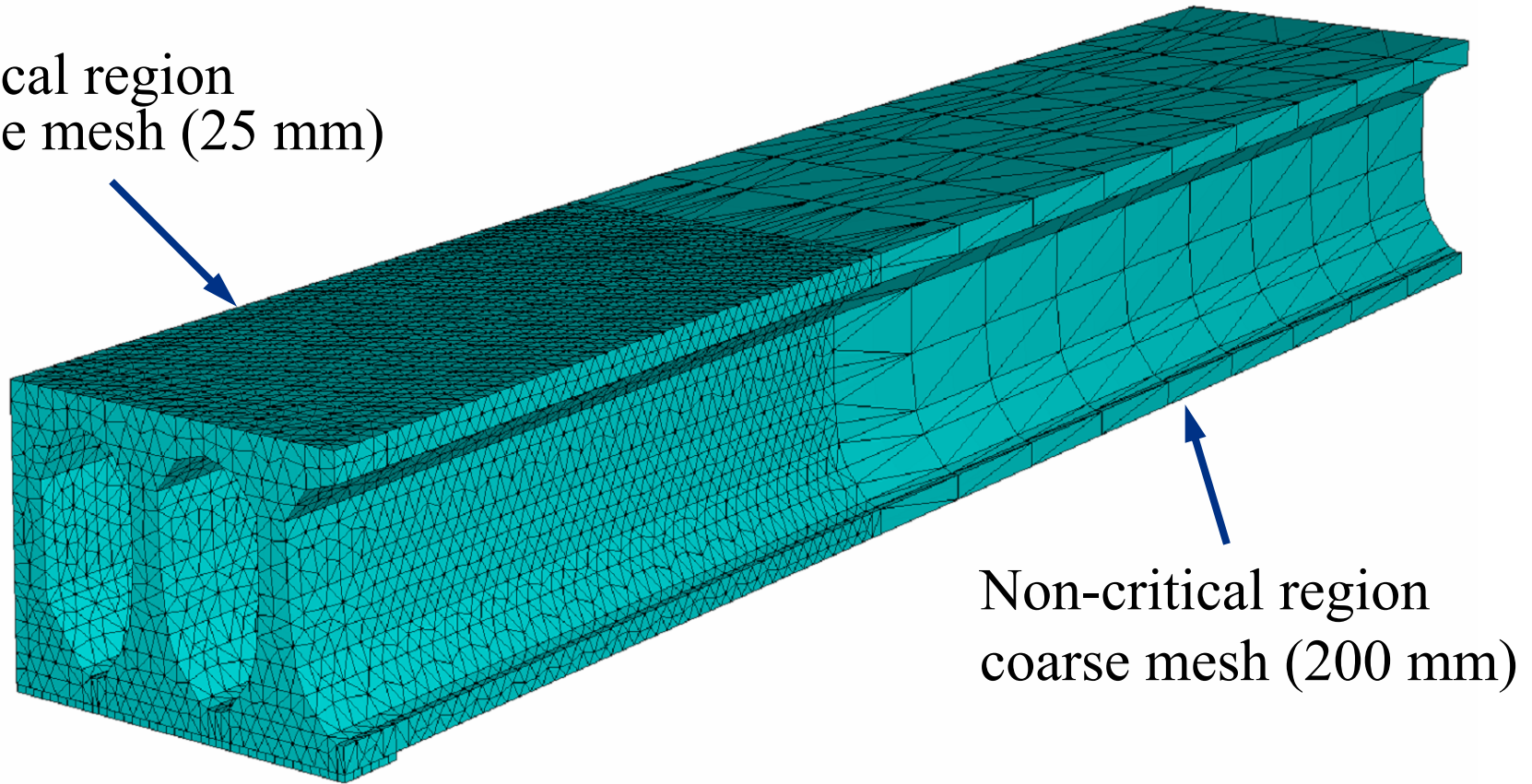
Initial stress from prestressing  
(initial condition)



Note that this is the stress distribution in the prestressing strands before “release”, i.e. before interacting with the concrete in the model.

# FE Model - Mesh

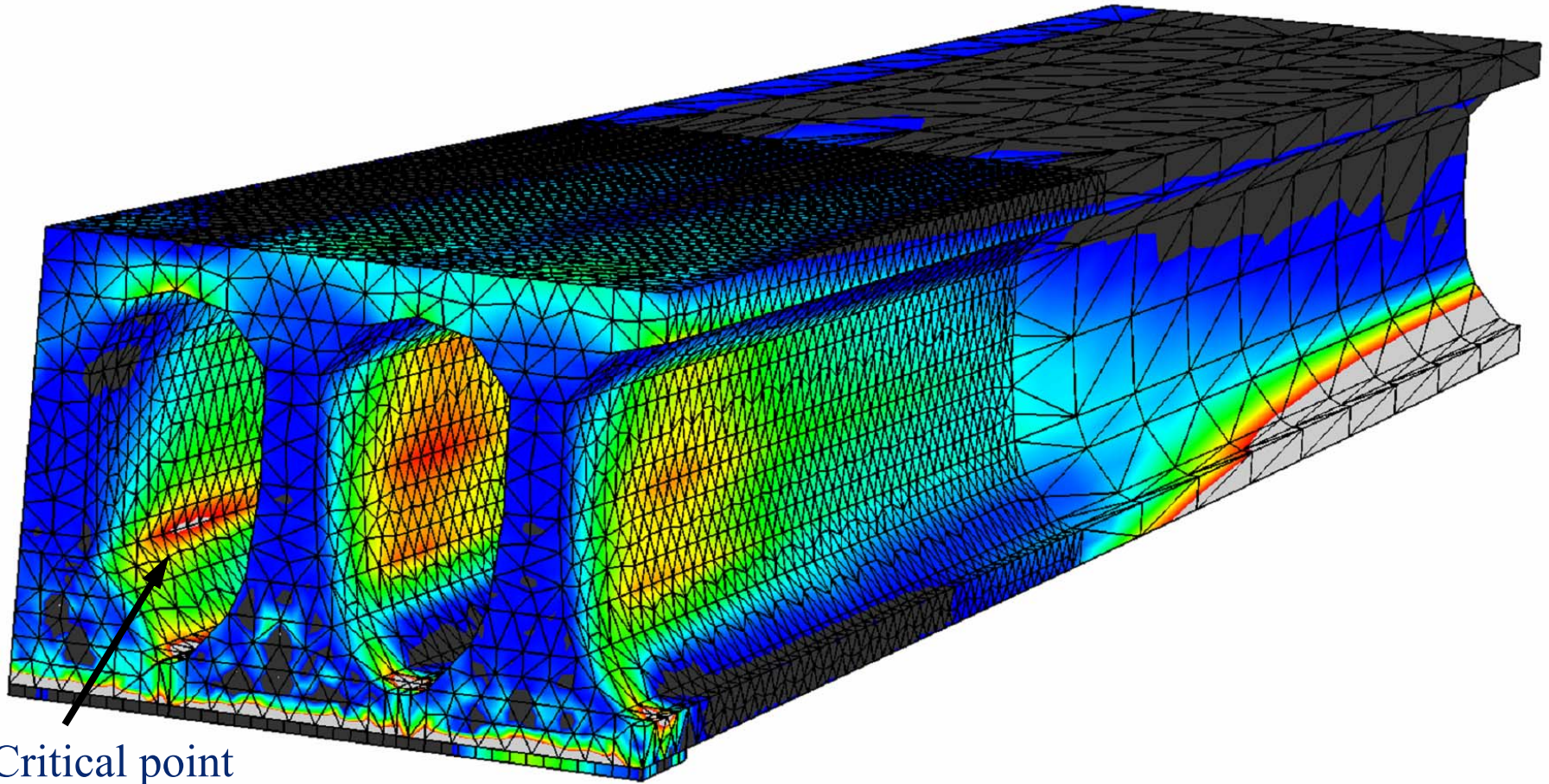
Critical region  
dense mesh (25 mm)



Non-critical region  
coarse mesh (200 mm)

# Results – FE Method

## Principal Stresses in the Reference case

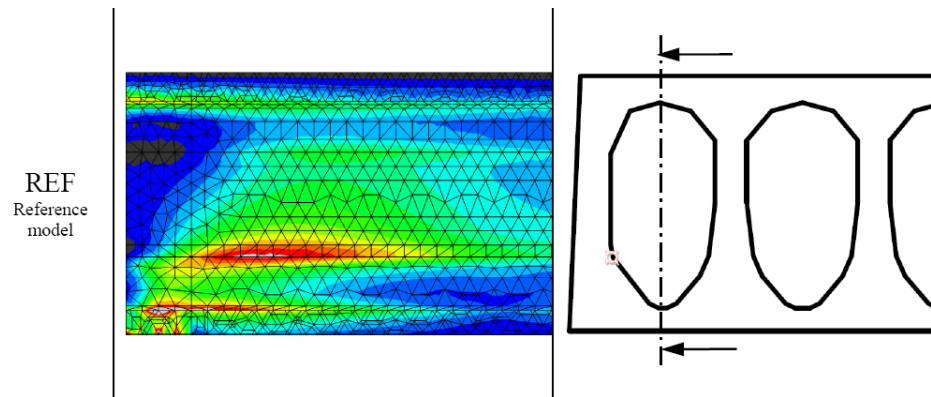


Critical point

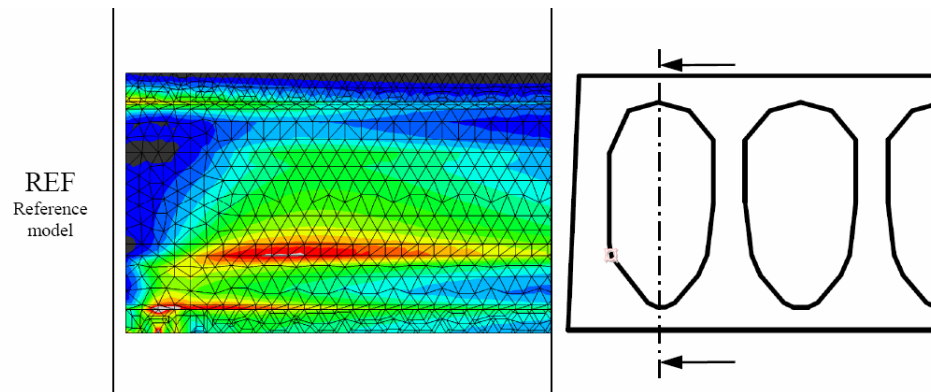
# Results – FE Method

## Stress Field in the Reference Case

**Short term response  
(28 days age)**



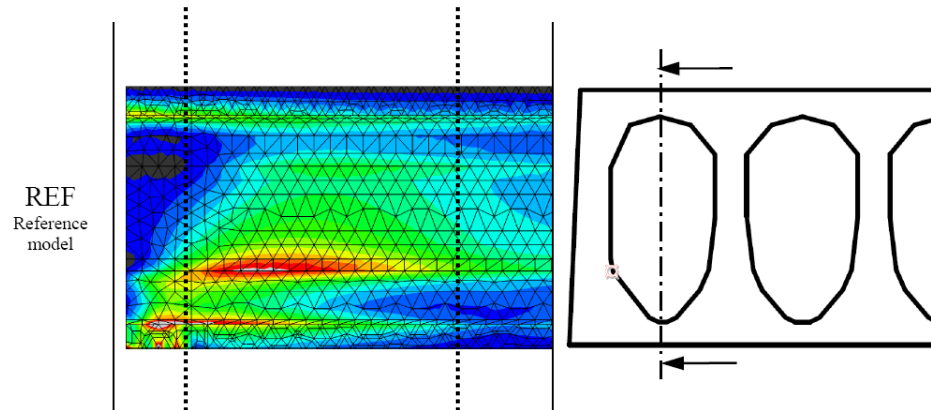
**Long term response  
(57 years age)**



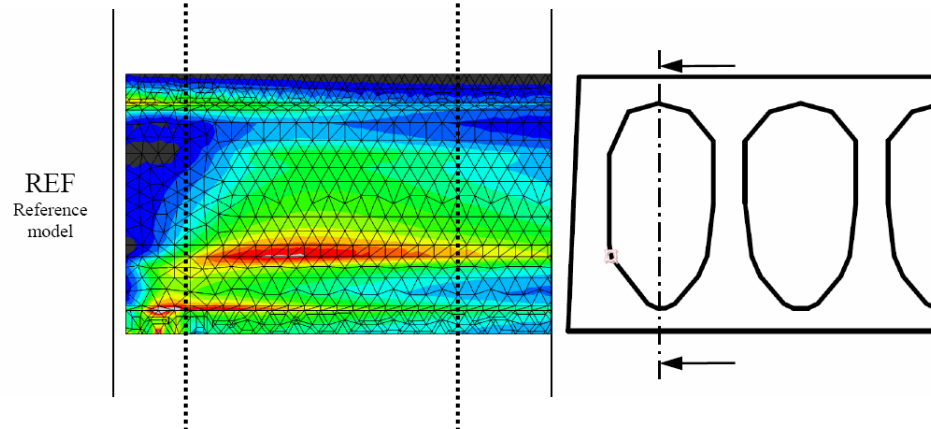
# Results – FE Method

## Stress Field in the Reference Case

**Short term response  
(28 days age)**

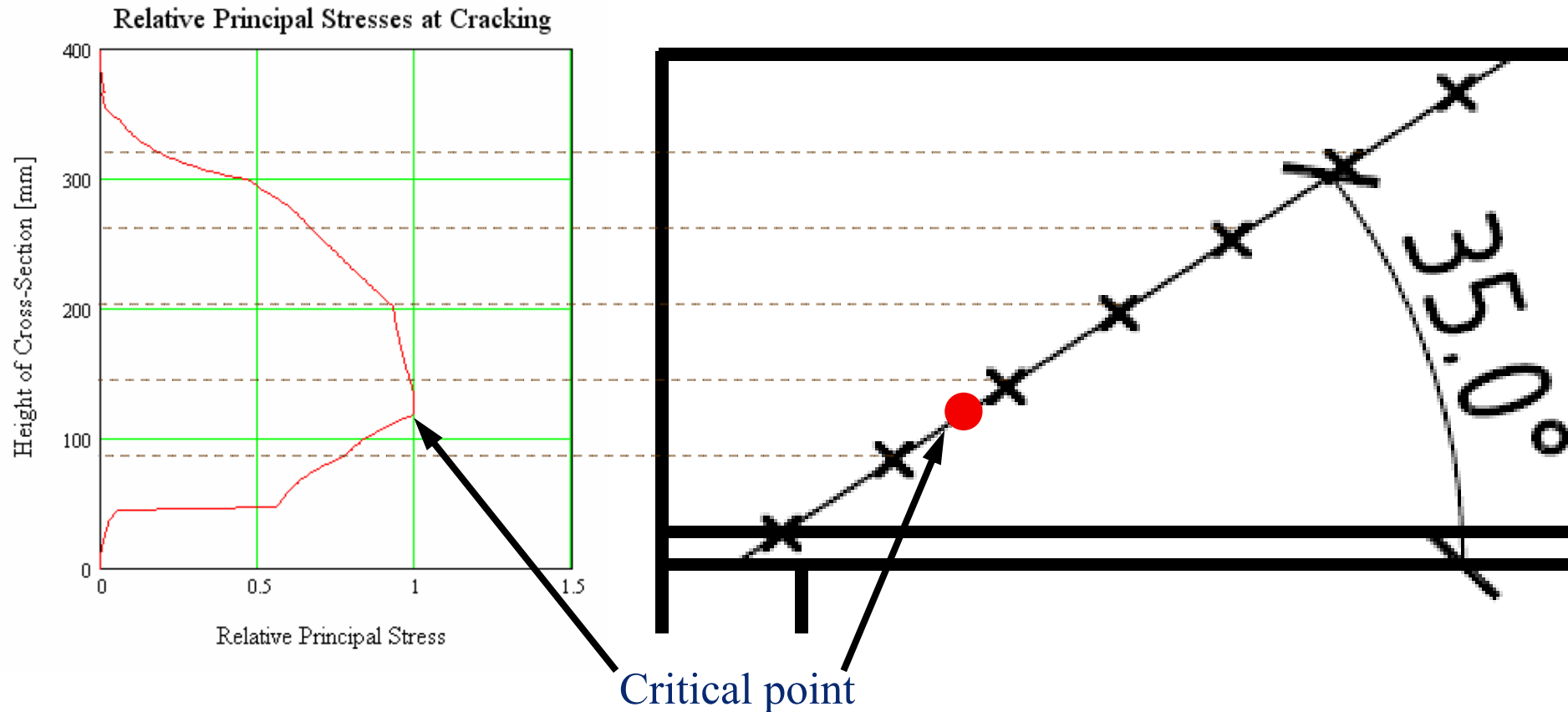


**Long term response  
(57 years age)**



# Results – Yang's Method

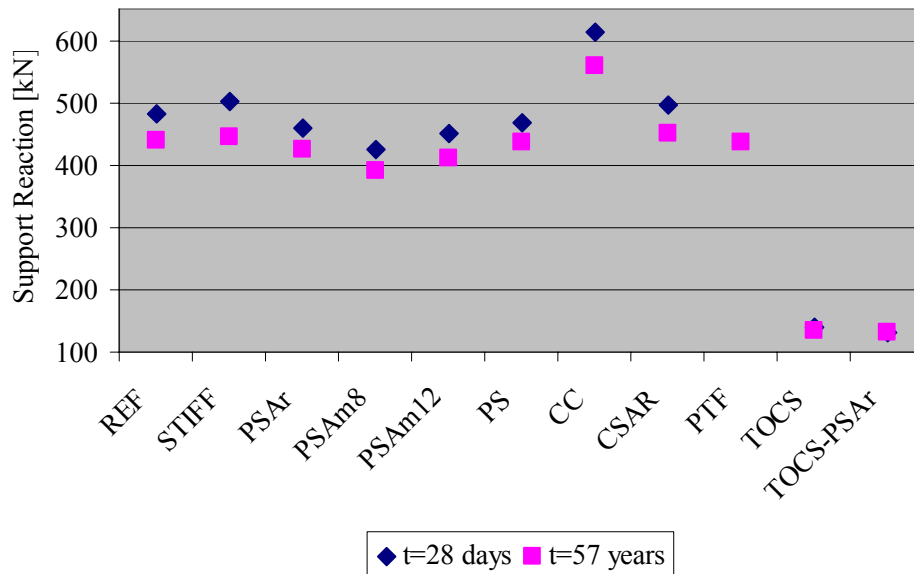
## Principal Stresses in the Reference Case



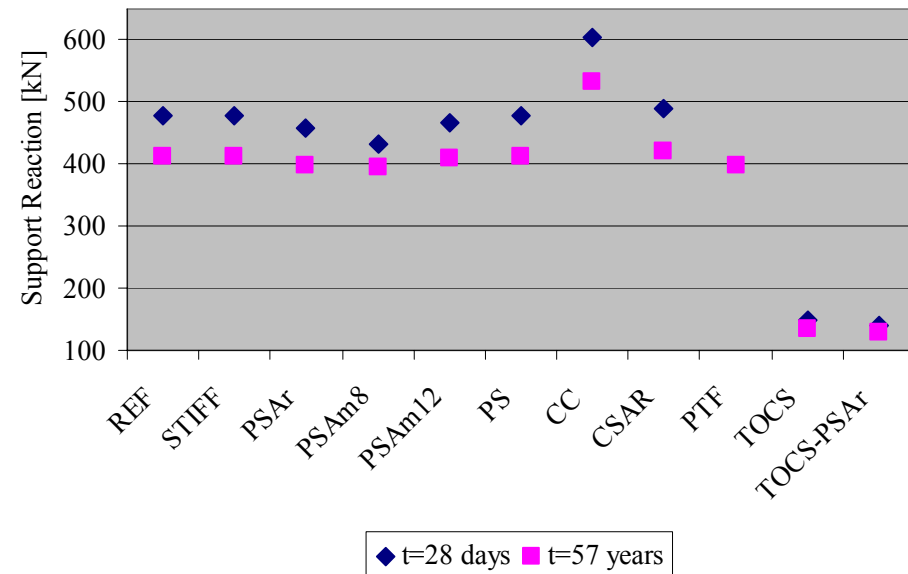


# Shear Capacity

Support Reaction at Web Shear Cracking  
FE Analyses

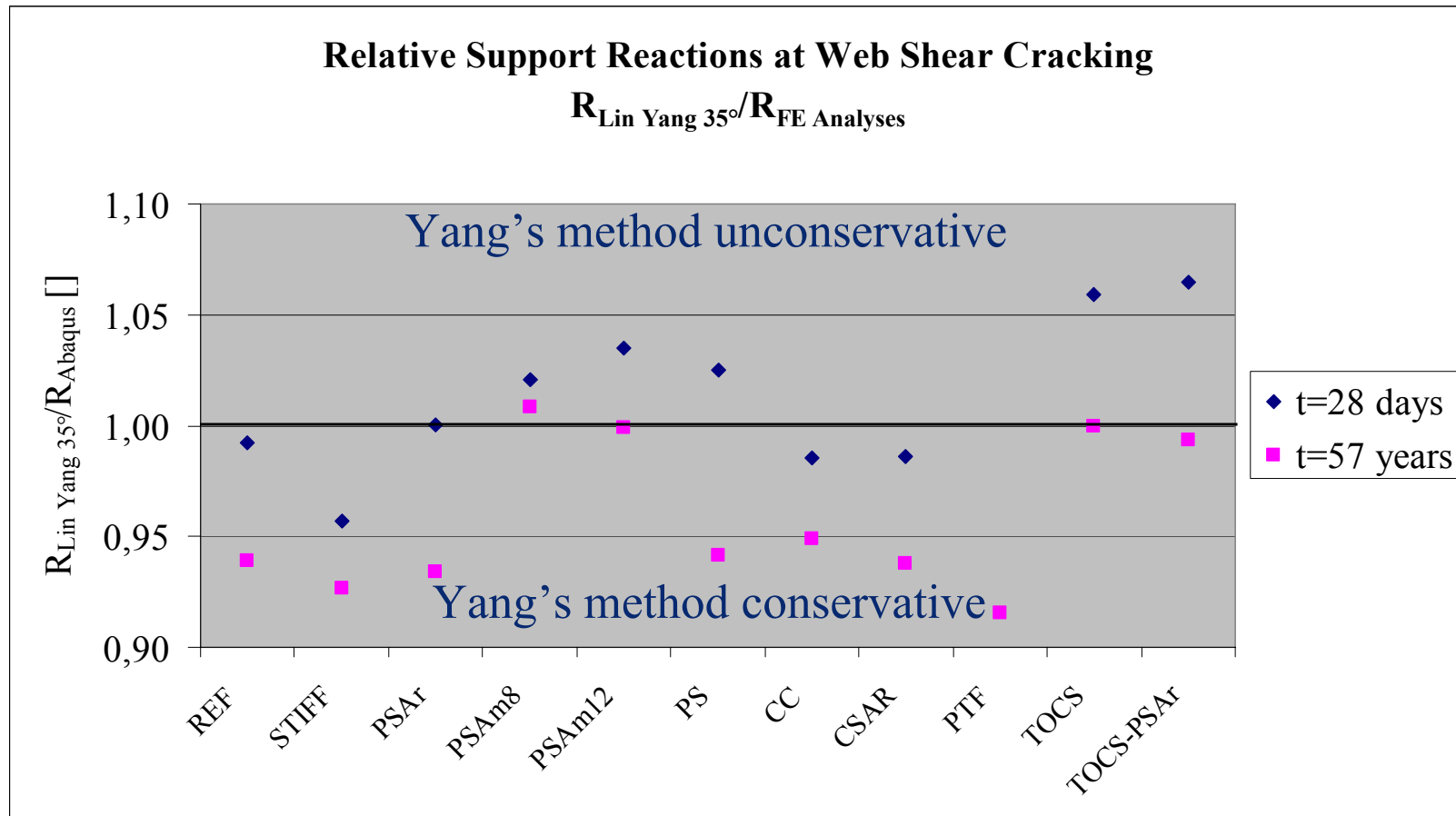


Support Reaction at Web Shear Cracking  
Lin Yang, 35° Critical Path from Mid Support

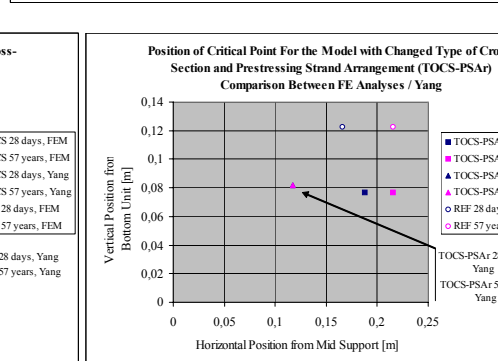
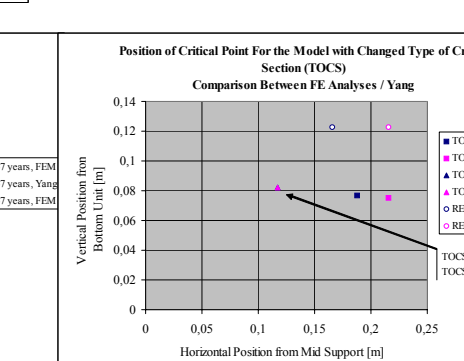
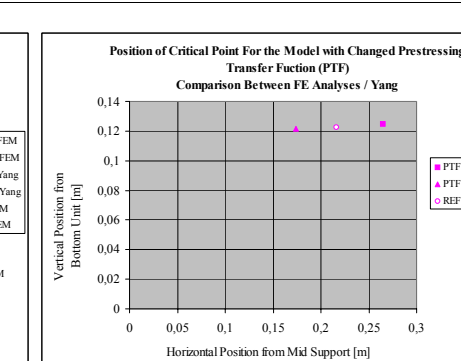
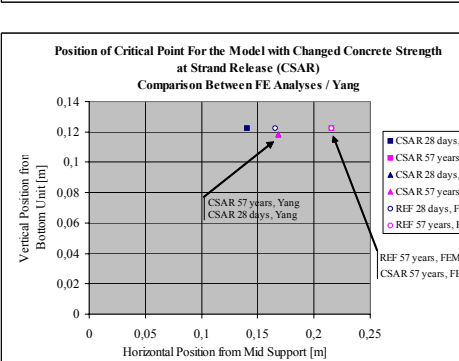
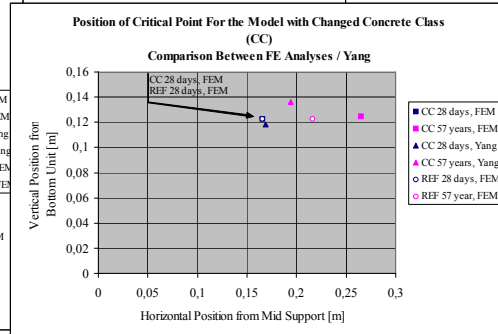
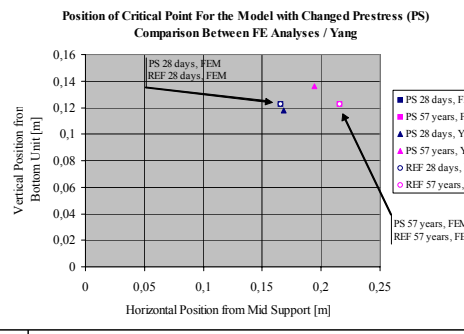
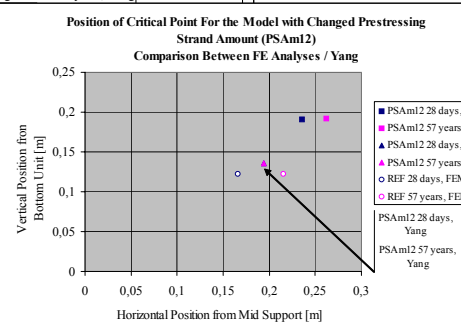
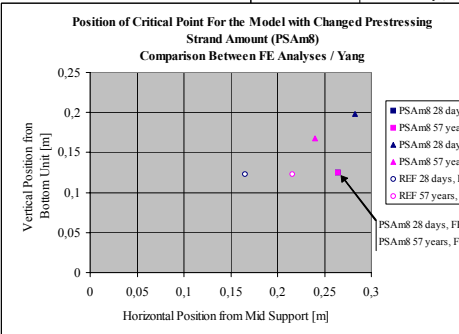
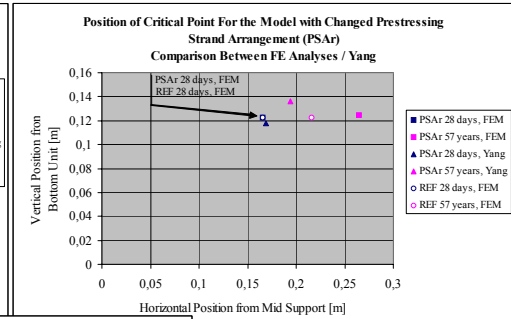
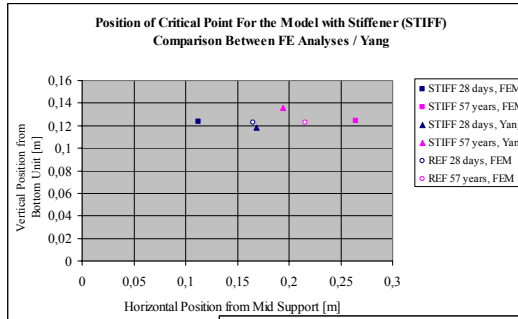
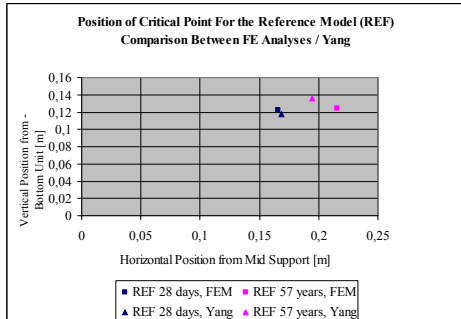


# Shear Capacity

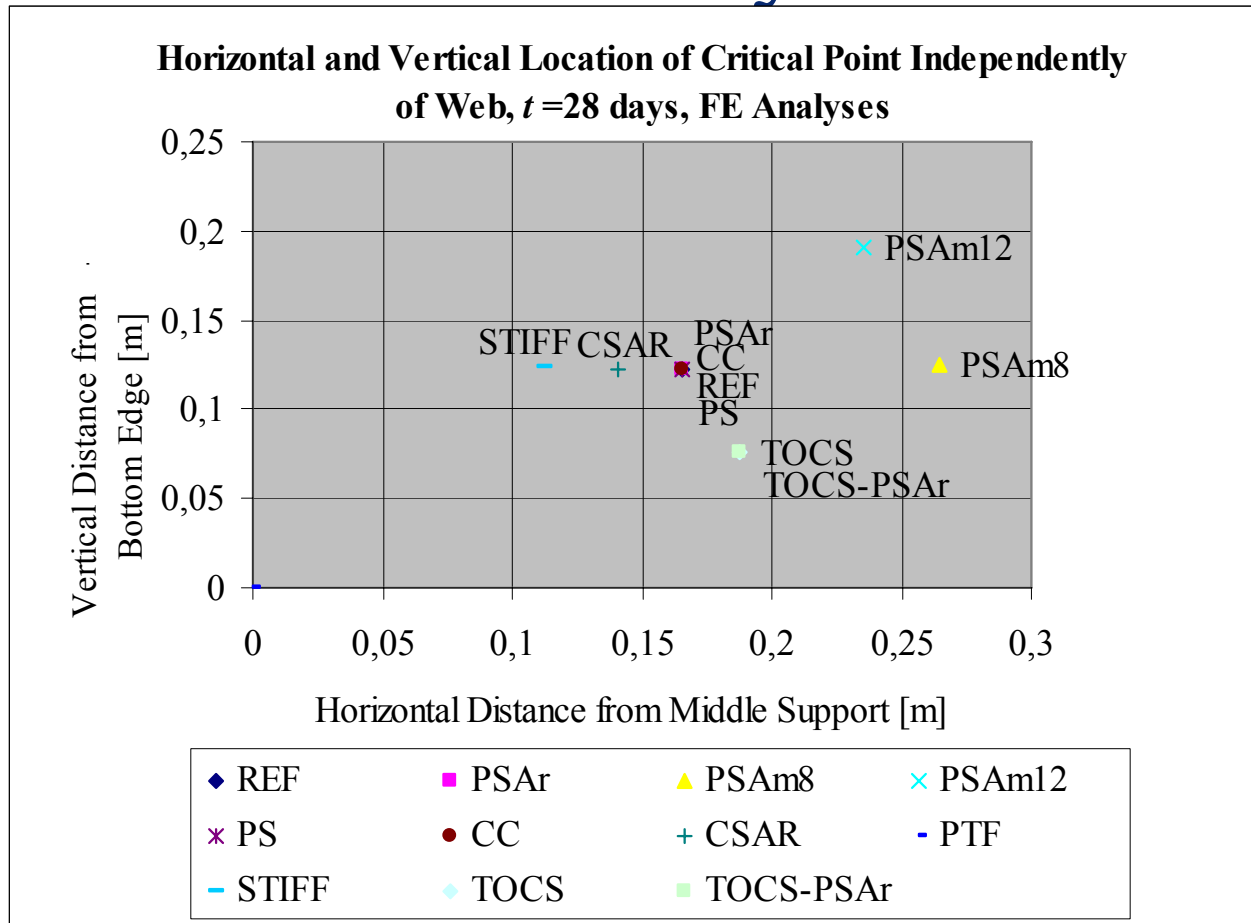
## Comparison between FEM and Yang's Method



# Location of Critical Point

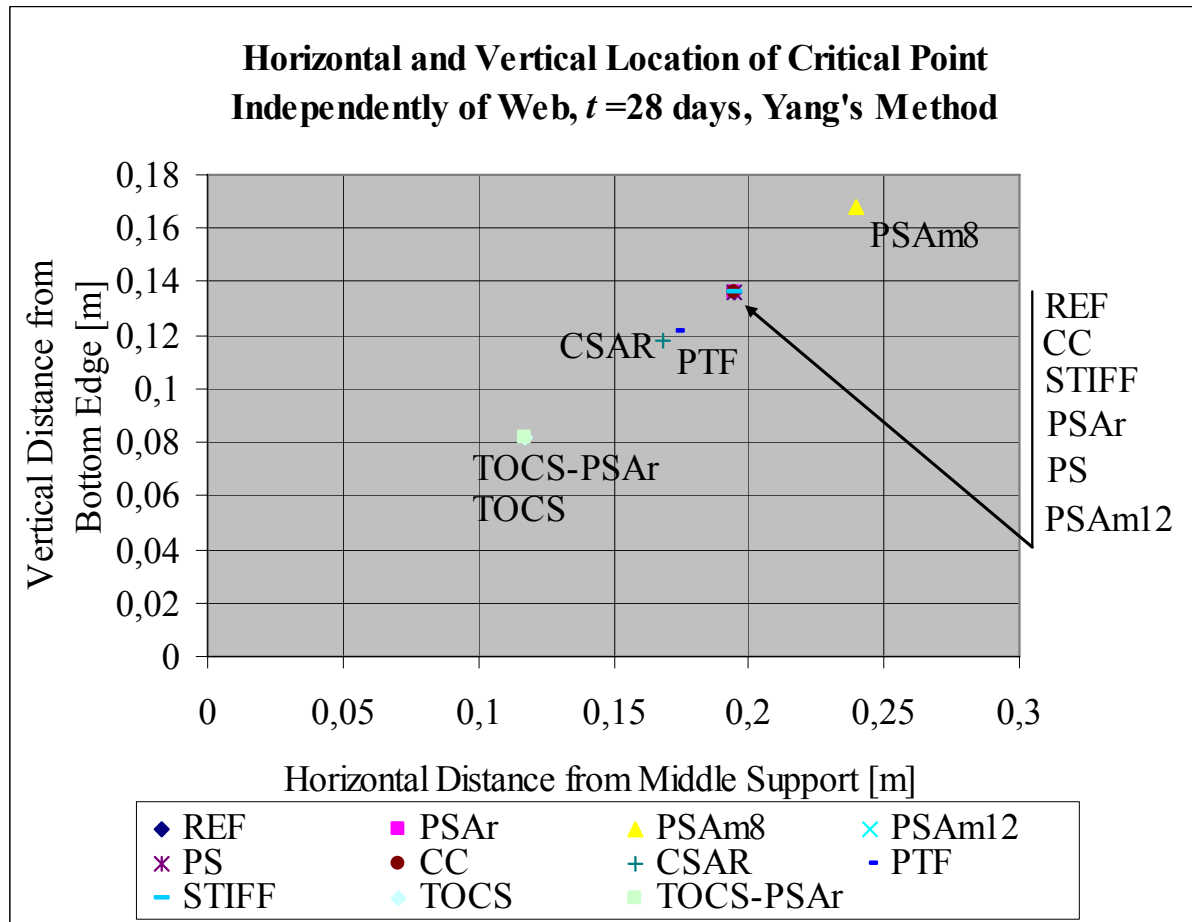


# Location of Critical Point FE Analyses

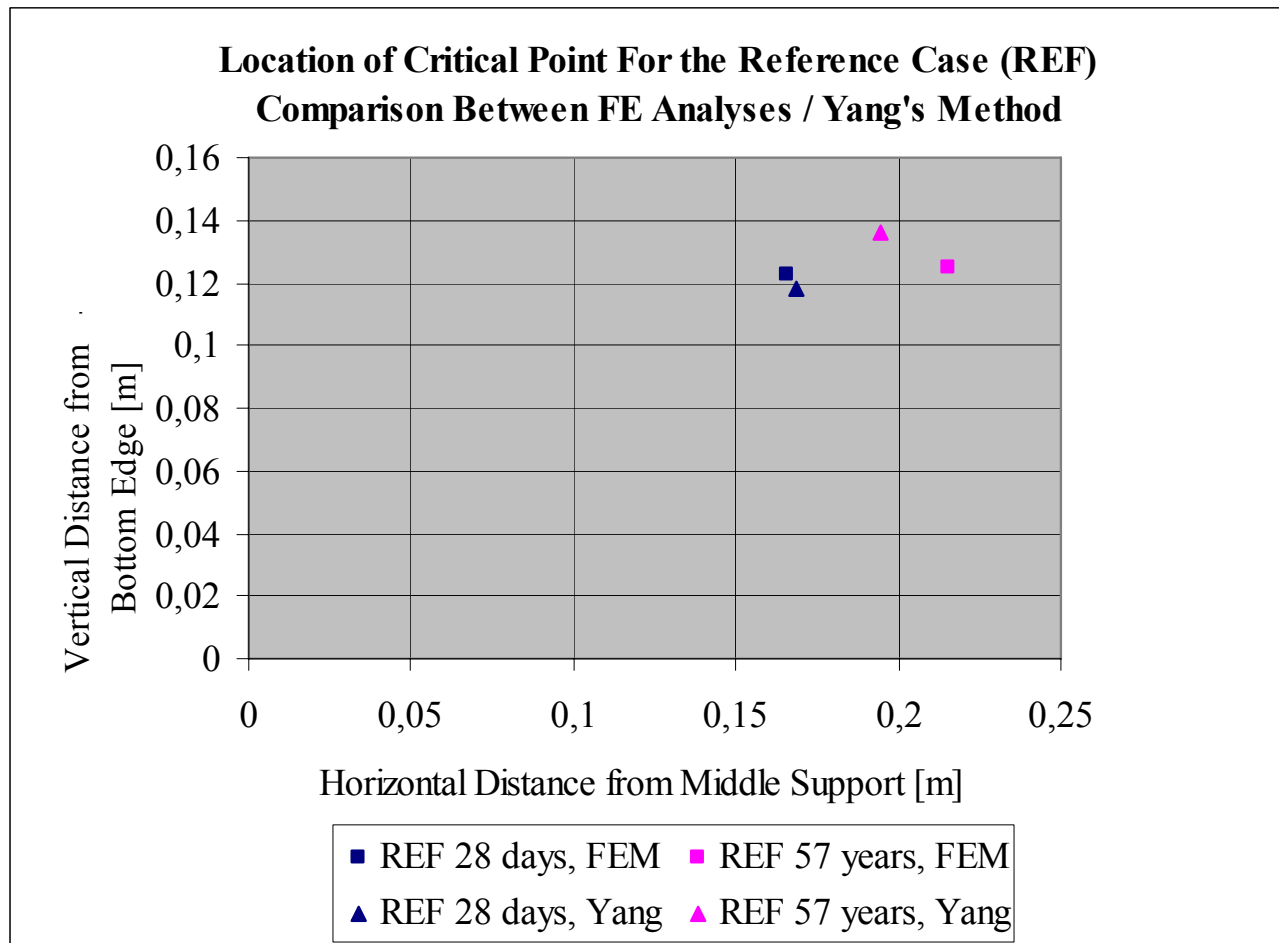


# Location of Critical Point

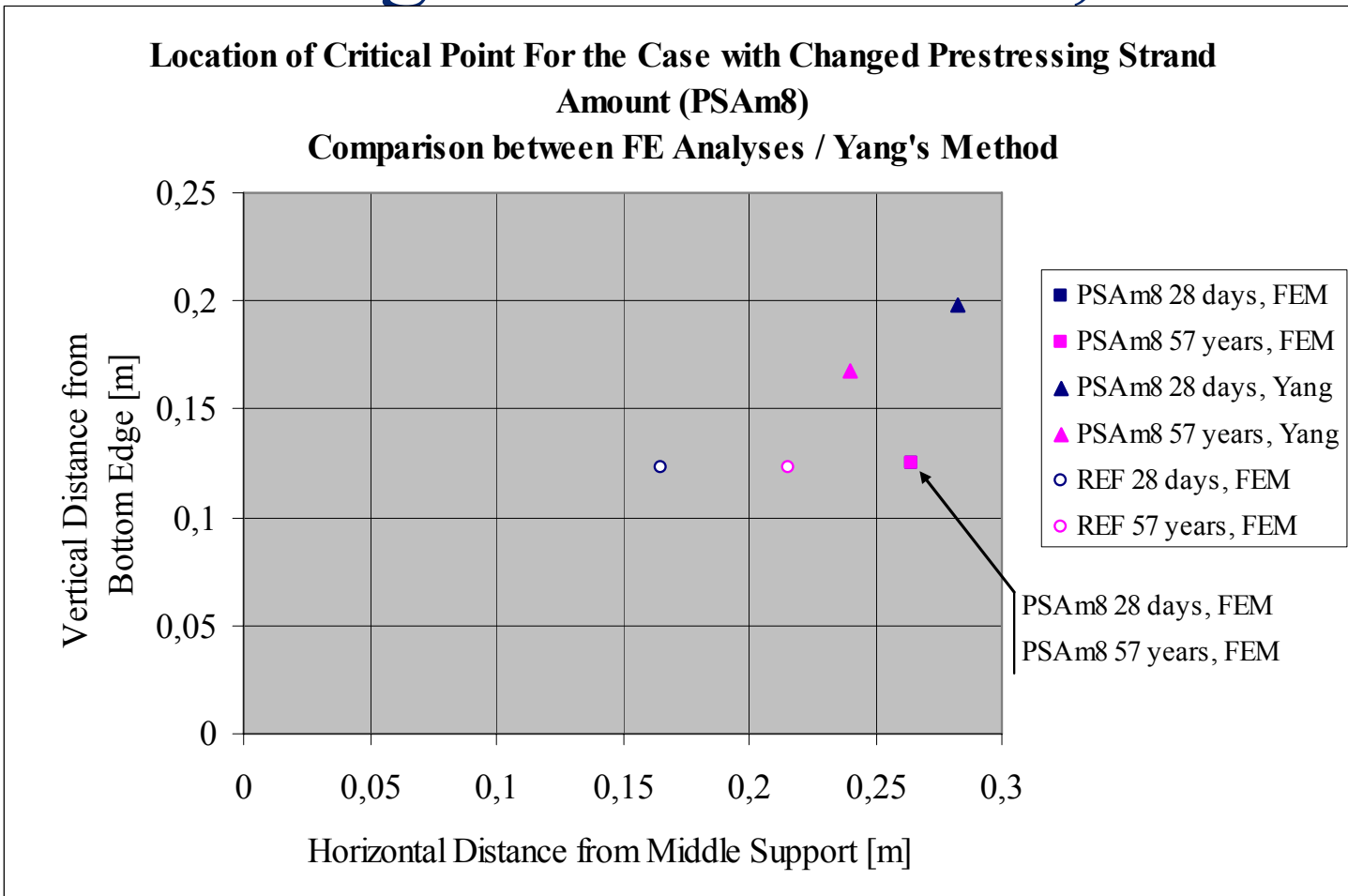
## Yang's Method



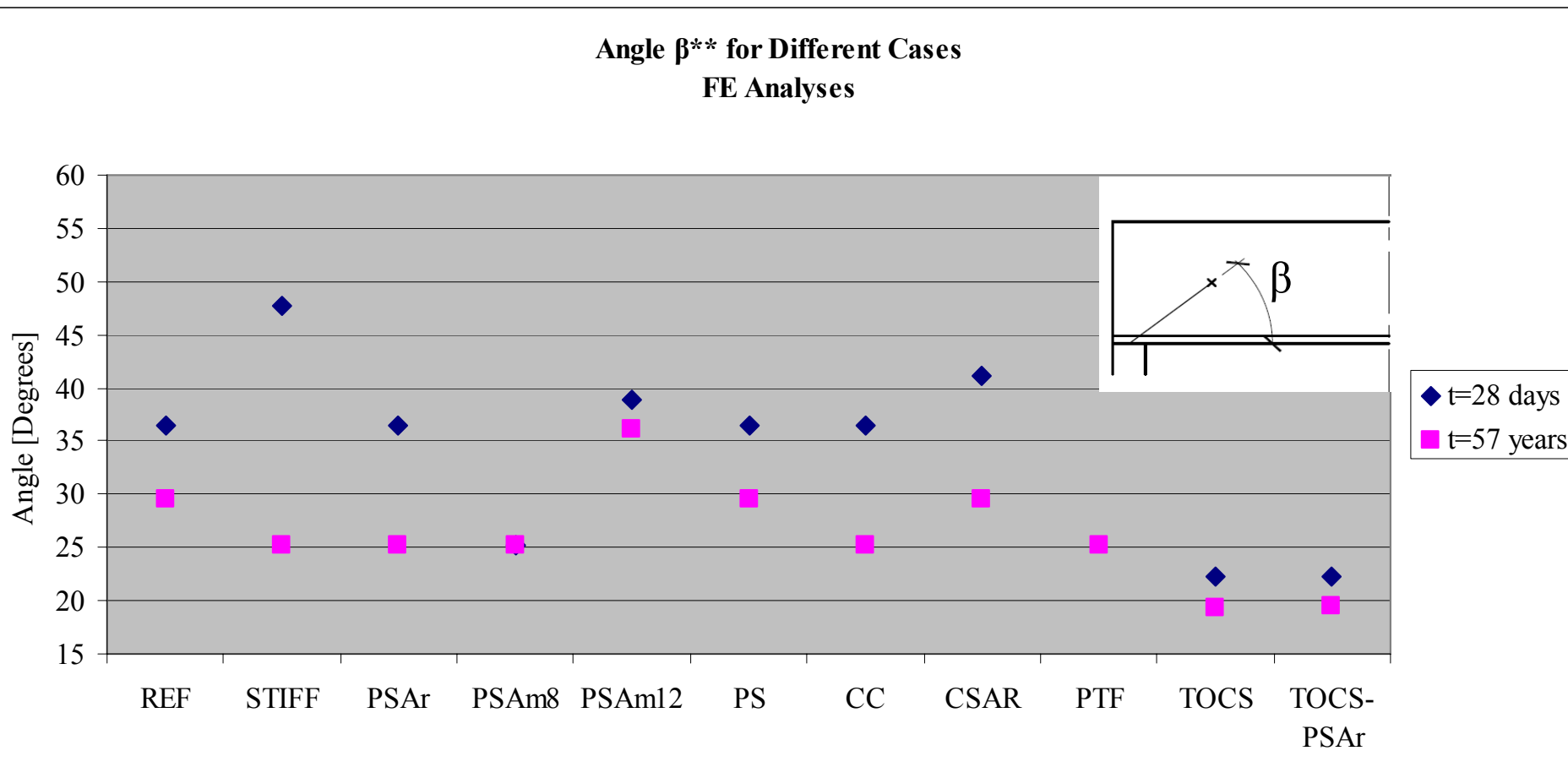
# Location of Critical Point: Reference Case



# Location of Critical Point: Prestressing Strand Amount, PSAm8



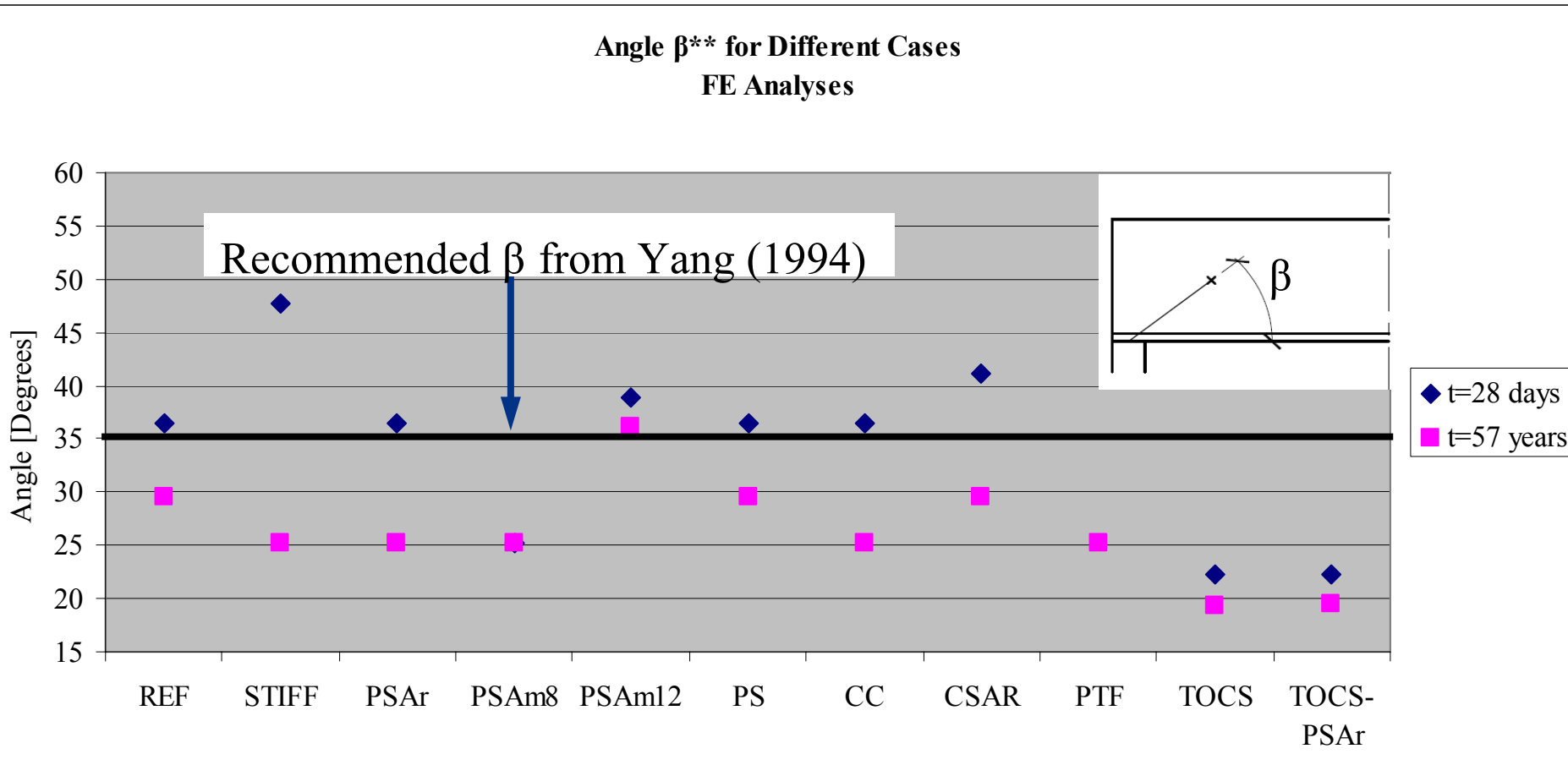
# Angle $\beta$ for Different Cases





# Angle $\beta$ for Different Cases

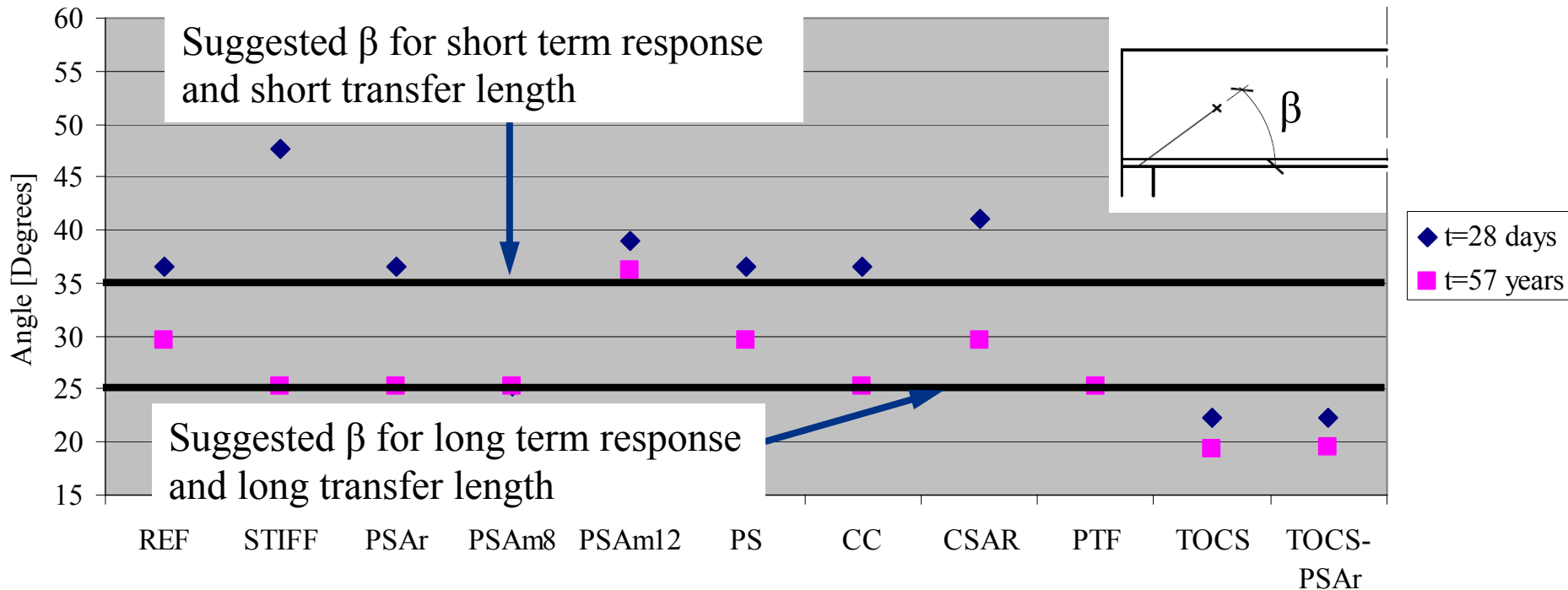
## Comparison between FEM and Yang's Method



# Angle $\beta$ for Different Cases

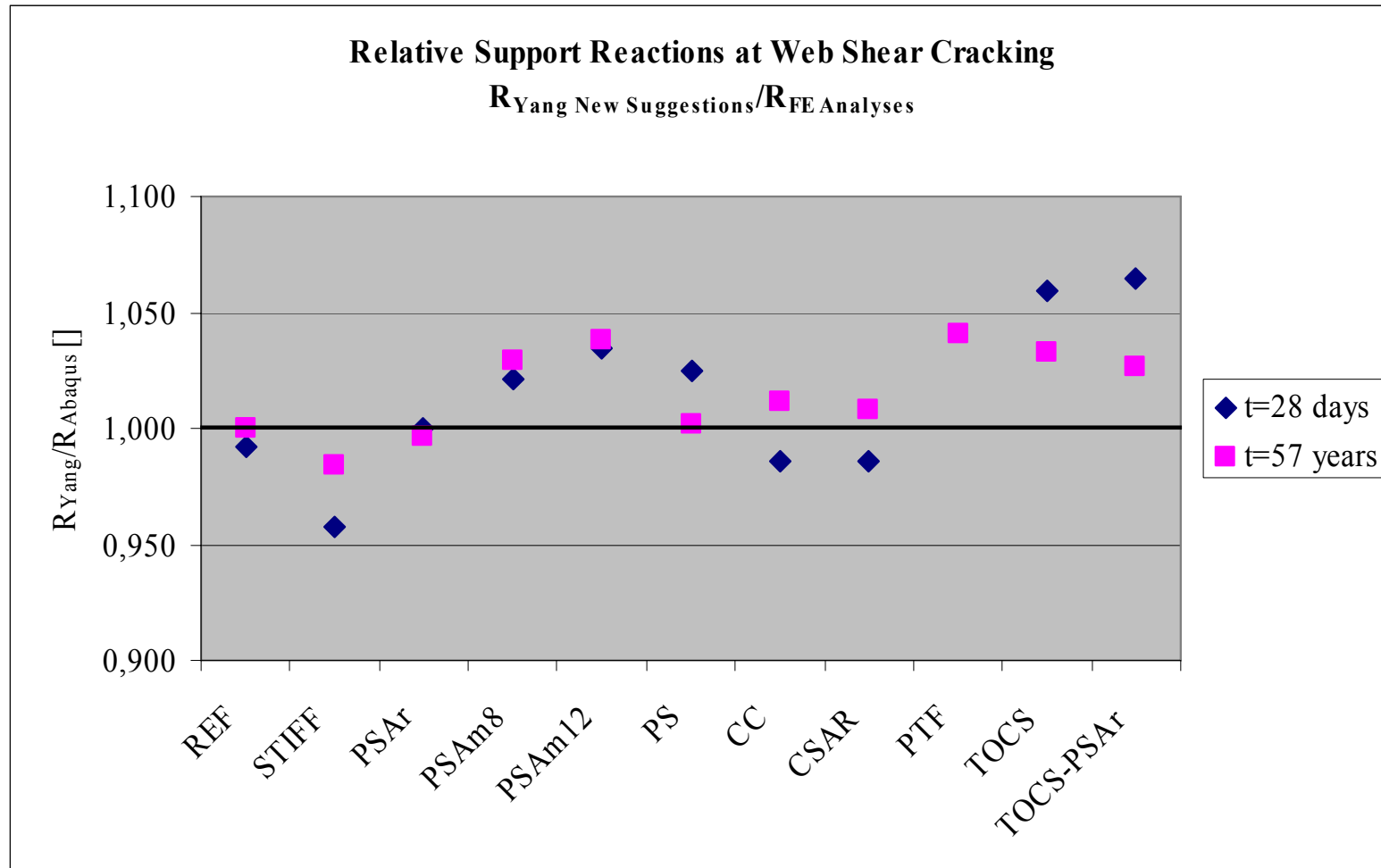
## Recommendations of New Angle

Angle  $\beta^{**}$  for Different Cases  
FE Analyses



# Relative Shear Capacity

## New Recommended Angle is Used



# Conclusions

## General from FE Analyses

- For long term response and long transfer length, the critical point was found along a path with a smaller inclination than  $35^\circ$  proposed by Yang (1994).
- For long term response and long transfer length, the capacity of web shear tension failure was reduced.

# Conclusions

## Specific from FE Analyses

- Decreased reinforcement amount had a great influence on the position of the critical point; the horizontal distance from the support to the critical point was increased. The capacity in web shear tension failure is reduced.
- Increased prestress from 1000 MPa to 1200 MPa did not affect the location of the critical point, but reduced the shear capacity.

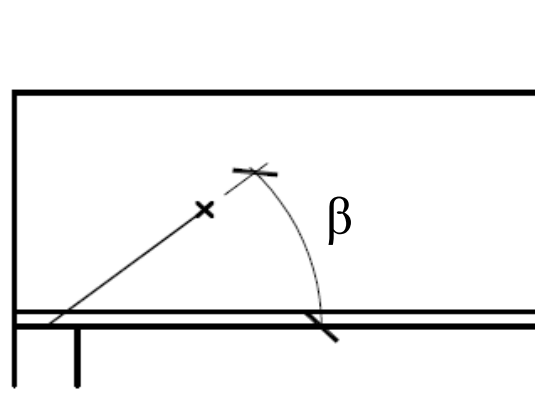
# Conclusions

## General from Comparison FEM – Yang's Method

- The agreement between Yang's method and FEM regarding the location of the critical point was, with some exceptions, good for short term response and short transfer length and less good for long term response and long transfer length.
- The agreement between Yang's method and FEM regarding the web shear tension capacity was, with some exceptions, good for short term response and short transfer length and less good for long term response and long transfer length.

# Recommendation

- Use  $\beta=35^\circ$  for short term response and short transfer length with Yang's method.
- Use  $\beta=25^\circ$  for long term response and long transfer length with Yang's method.



# Thanks for your attention!

