

# Design of hollow core floors - Dynamic behaviour

Vibrations, fatigue

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# Dynamic actions

- Vibrations
  - Gyms (Sports- and dance halls)
  - *Machine foundations*
  - *Climate related actions (wind)*
- Fatigue
  - Floors subjected to traffic loads (Trucks and forklift-trucks)
  - Park decks
  - *Machine foundations*
  - *Climate related actions (wind)*

# Vibrations

## Sports and dance halls

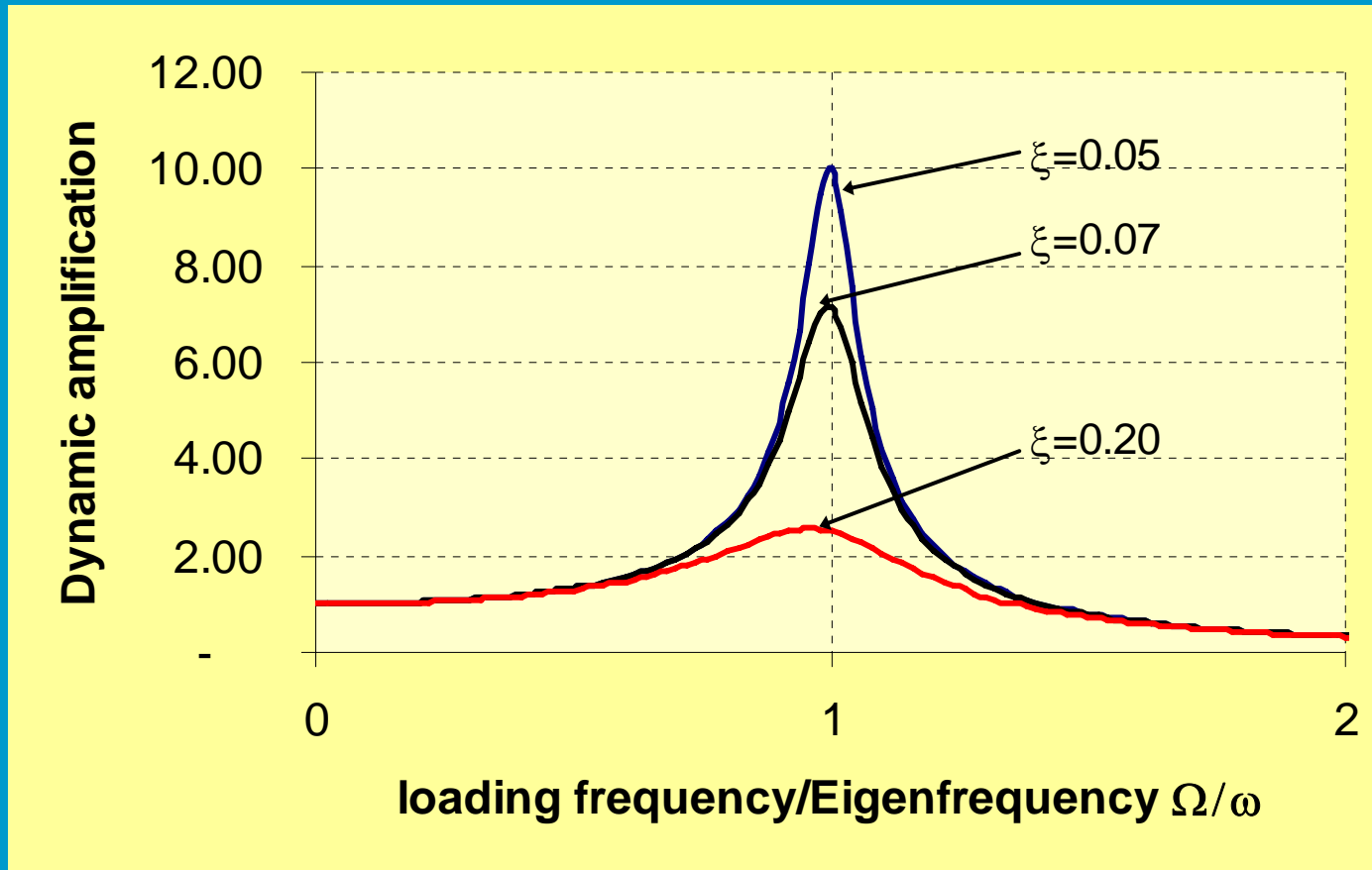


Problem: with a standard design in accordance with building codes resonance phenomena can still occur



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# Resonance



Significant deformation increase!

# Design by frequency tuning

Structure type	Sports halls	Dance halls
Reinforced concrete	$f_1 > 7.5$ Hz	$f_1 > 6.5$ Hz
Prestressed concrete	$f_1 > 8.0$ Hz	$f_1 > 7.0$ Hz
Composite	$f_1 > 8.5$ Hz	$f_1 > 7.5$ Hz
Steel	$f_1 > 9.0$ Hz	$f_1 > 8.0$ Hz

After: Bachmann u.a. [1995], Vibration Problems in Structures, Practical Guidelines

Many national codes (eg. DIN 1045-1 do **not** have **frequency limitations!**

# Eigenfrequency of hollow core slabs

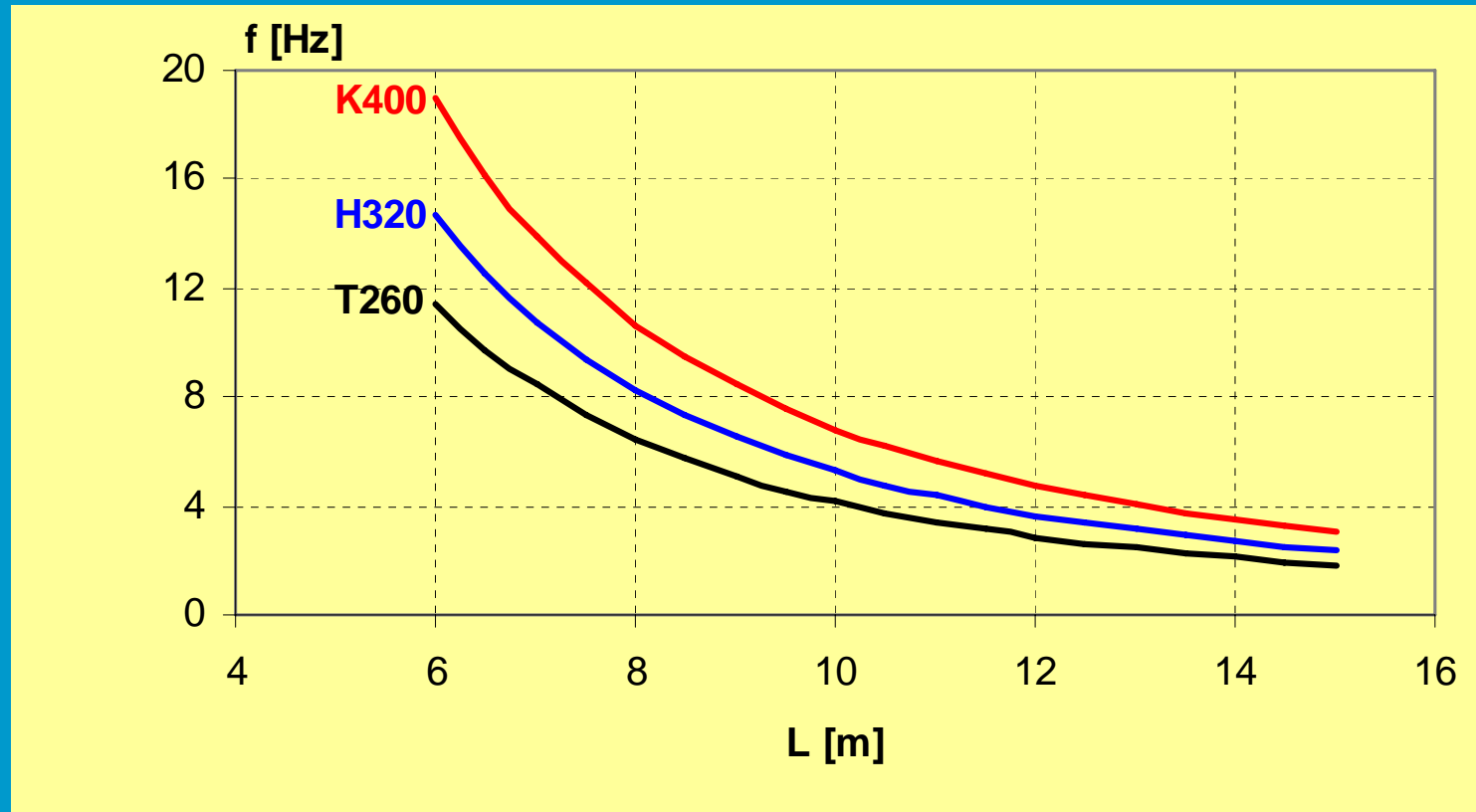
Simply supported beam:



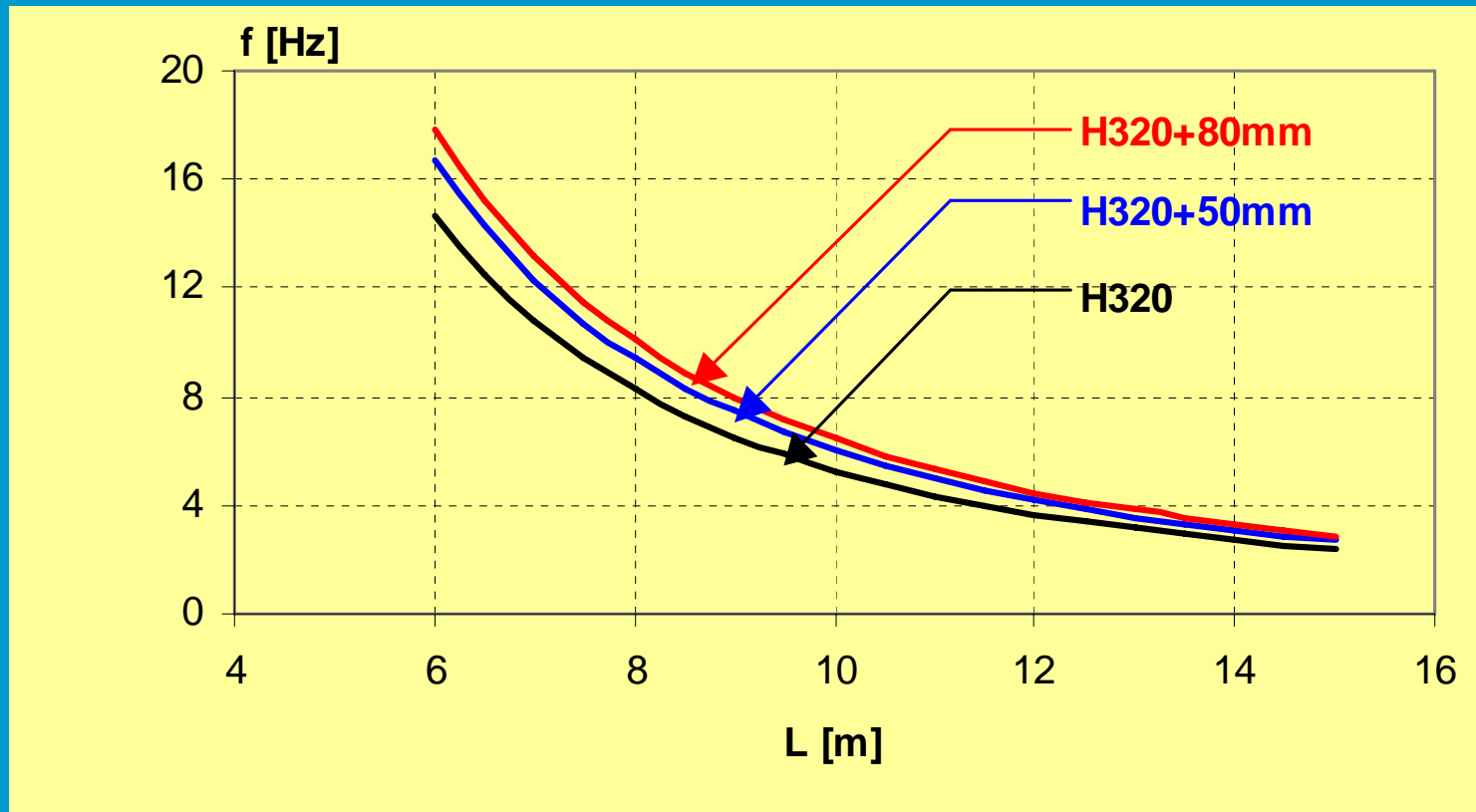
$$f_1 = \frac{\pi}{2 \cdot l^2} \cdot \sqrt{\frac{E \cdot I}{m}}$$

More accurate determination of frequency possible if requested (dynamic analysis, FEM) – but input data should be determined as accurate as possible!

# Frequency of hollow core slabs



# Influence of a topping





# Methods to reduce vibrations in existing structures

- Increase of Mass/Stiffness
- Increase of damping

**Expensive!!**



London Millennium Bridge:  
160 people – 70mm lateral displacement.

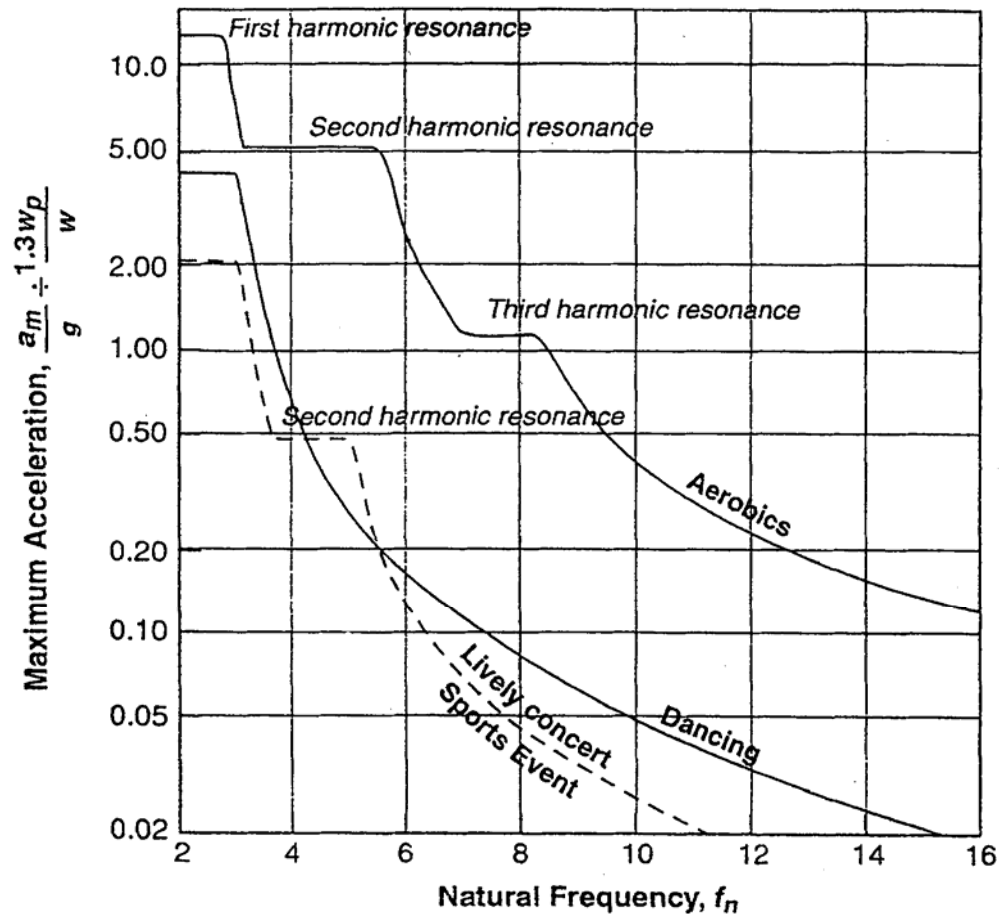
37 viscous dampers  
52 tuned massed dampers

**£4** million additional costs!

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# Guideline: ATC Design Code 1 Minimizing Floor Vibration



- Acceleration limits, for walking, but also rhythmic activities (Aerobics)

- Required values of eigenfrequencies for rhythmic events

# Conclusions (vibrations):

- Eigenfrequency of hollow core slabs can be determined by simple supported beam formula – gives a reliable first estimate and can serve to point out critical design situations (for SLS).
- More complicated cases require a complete dynamic analysis.

# Traffic loads

## Parkdecks

Design as required by building codes.



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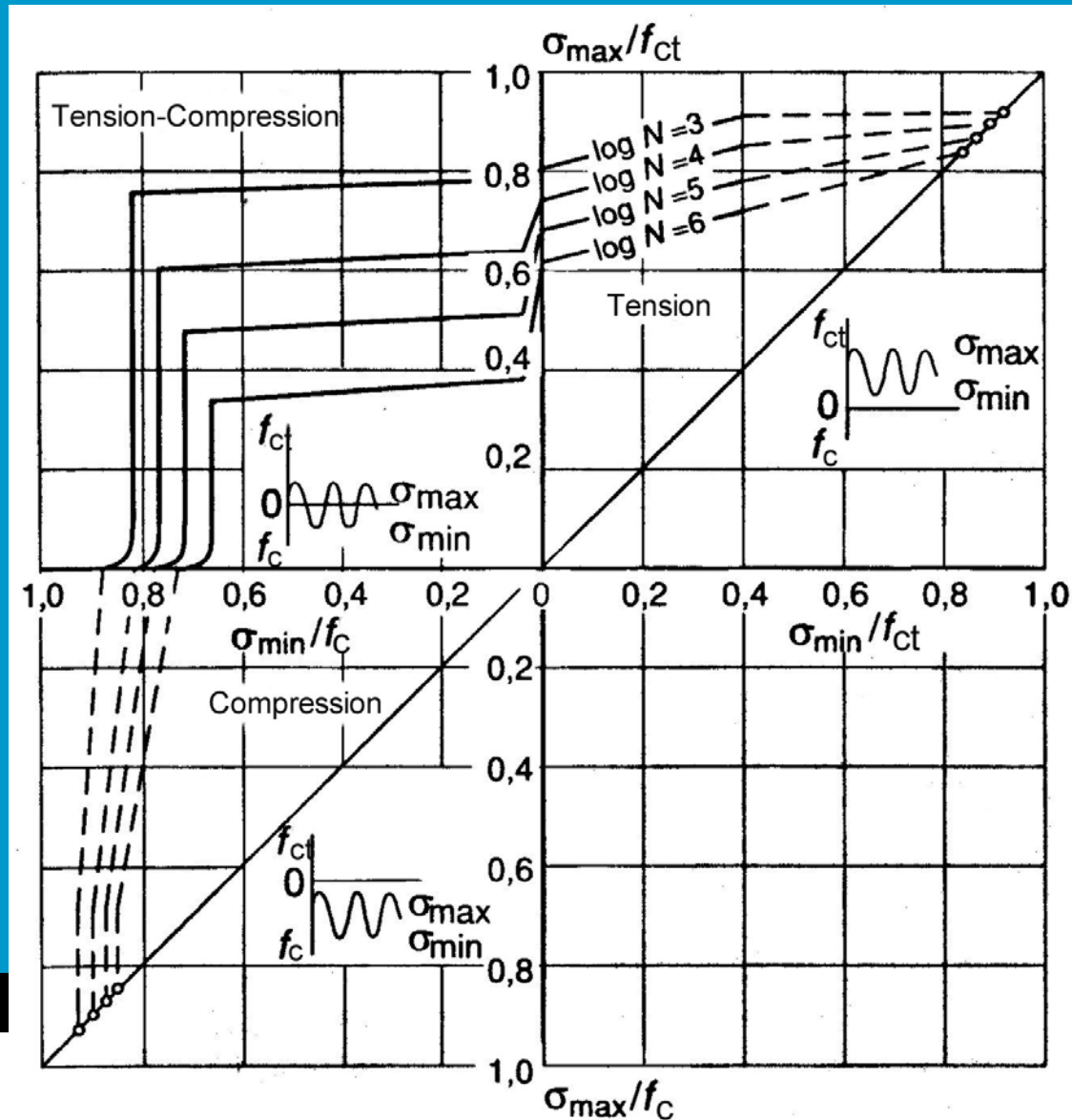
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# Floors subjected to traffic by trucks and forklift trucks

First case in the Netherlands: flower auction hall Westland, limited truck traffic allowed.

Fatigue verifications; critical failure mode:  
Shear tension failure

# Fatigue of Concrete



# Fatigue verifications in EC2

- Verifications form part of ULS.
- Separate verifications for reinforcing steel and concrete.
- Simplified verifications: Stress limitations (of max. compressive strength in concrete or max. shear force in concrete – with use of SLS load combinations and safety factors.
- Verifications with S-N lines for steel and concrete and with Palmgren Miner sum for damage accumulation.

**But: No verifications for concrete under **tension!****

# Shear tension failure & fatigue

Static case:

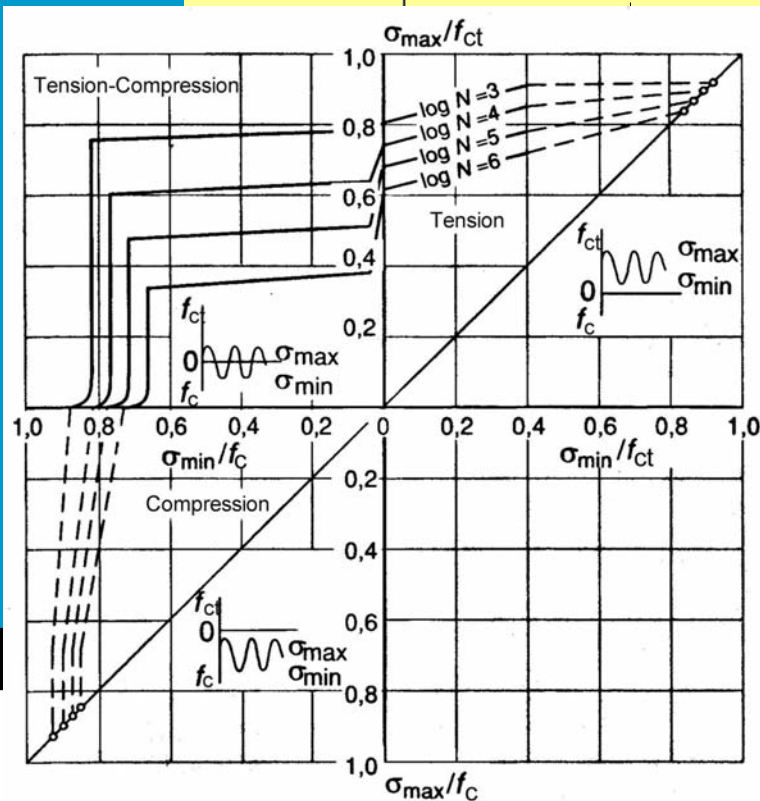
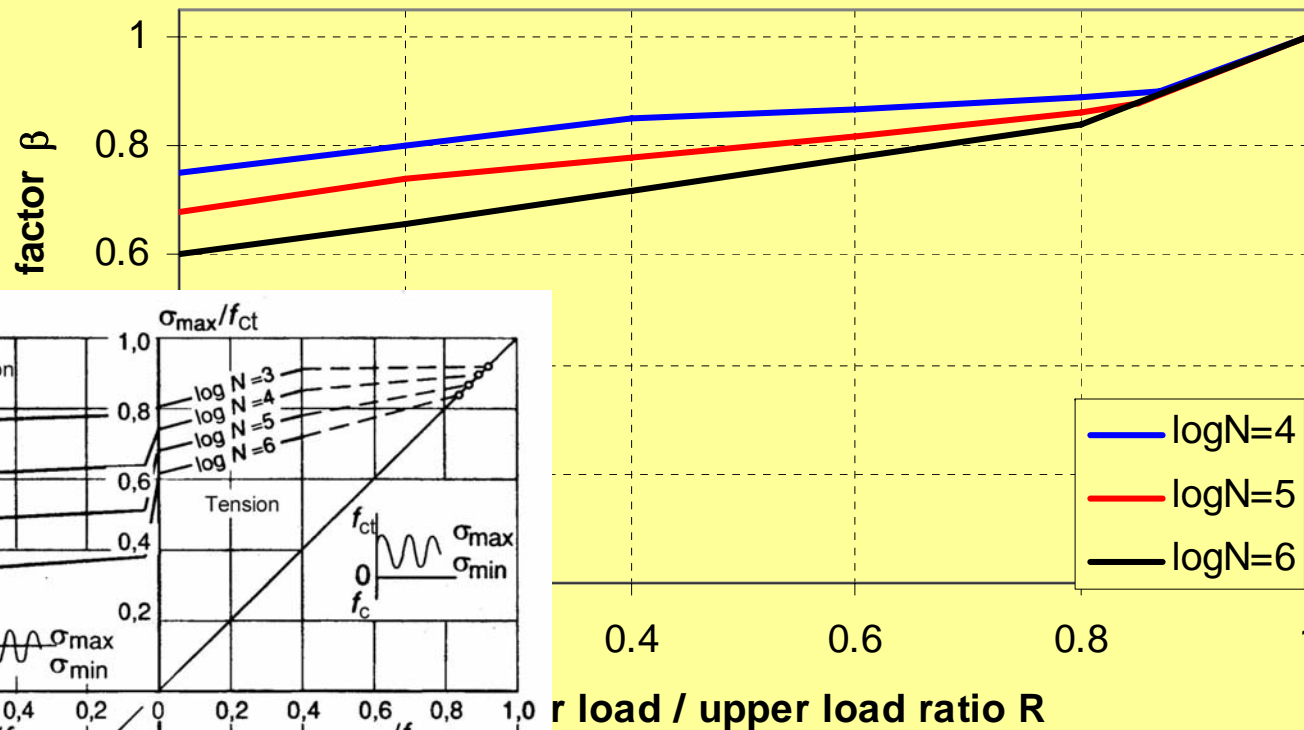
$$V_{Rd,ct} = \frac{I \cdot b_w}{S} \sqrt{\left( \frac{f_{ctk;0.05}}{\gamma_c} \right)^2 - \alpha_1 \cdot \sigma_{cd} \cdot \frac{f_{ctk;0.05}}{\gamma_c}}$$

Fatigue: reduction of tensile strength by  $\beta_Z$ :

$$V_{Rd,ct,red} = \frac{I \cdot b_w}{S} \cdot \sqrt{\left( \frac{\beta_Z \cdot f_{ctk;0.05}}{\gamma_c} \right)^2 - \alpha_1 \cdot \sigma_{cd} \cdot \frac{\beta_Z \cdot f_{ctk;0.05}}{\gamma_c}}$$



# Reduction factor $\beta_Z$



# Other verifications

- For other failure modes static design as in codes; in case of traffic loading that can cause fatigue failure additional fatigue verifications needed.
- Fatigue verifications for these failure modes are covered by building codes (EC2).

# Conclusions

- Hollow core slabs for dynamic actions (sports- and dance halls): frequency tuning recommended, even though it is not explicitly required in the codes. A frequency tuned structure will be less affected by vibrations which can limit the serviceability of a structure, and can prevent expensive correction measures.

# Conclusions

- Floors subjected to traffic might need fatigue verifications. These are covered by the codes for most failure modes except shear tension failure. It is recommended to include this failure mode by reducing the concrete tensile strength, as presented here.

Relevant publication:  
Concrete plant & precast technology  
(BFT)

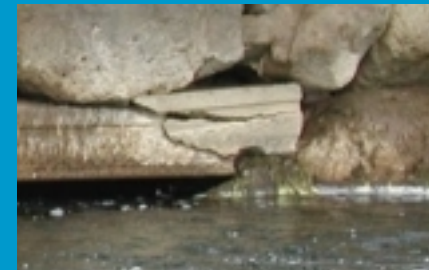
Walraven, Lappa: Precast prestressed  
hollow core floors subjected to dynamic  
loading (5/2004)

<http://www.bft-online.info/en/>

# Hauptversagensarten von Spannbetonhohlplatten

- Reines Biegeversagen
- Schubzugbruch
- Biegeschubbruch
- Verankerungsbruch
- Schubversagen in den Plattenlängsfugen

Kritisch bei Ermüdung!



# Abminderungsbeiwert $\beta_Z$

$$\beta_Z = 0.6 \text{ für } N=10^6 \text{ und Unterspannung } \sigma_{\min} = 0 \\ (R = 0)$$

Anzahl Lastspiele bis zum Bruch N anhand von zu erwartender Verkehrsbelastung im Betrieb bestimmen

Nachweis empfohlen, da DIN 1045-1 keine Ermüdungsnachweise für Beton unter Zug enthält